



THE 3000 METER TOWER

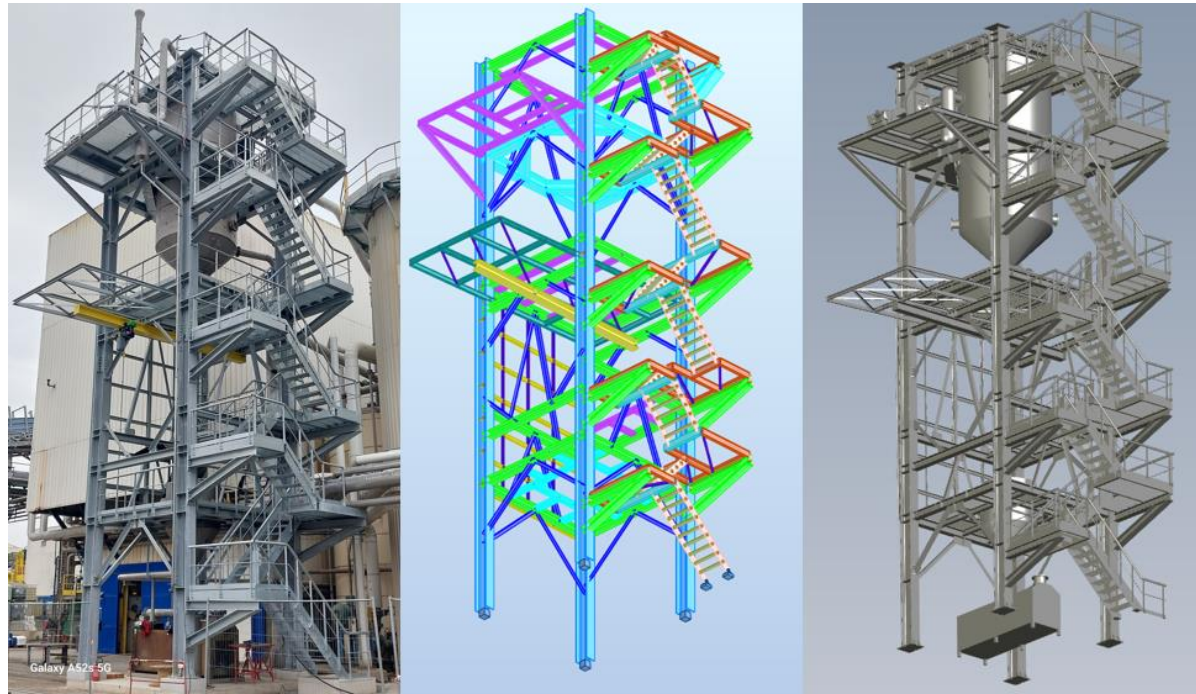
COMPAGNIE GÉNÉRALE DE L'INDUSTRIE (CGI)

sebastien.besse@cgindustrie.com

www.cgindustrie.com

COMPAGNIE GÉNÉRALE DE L'INDUSTRIE

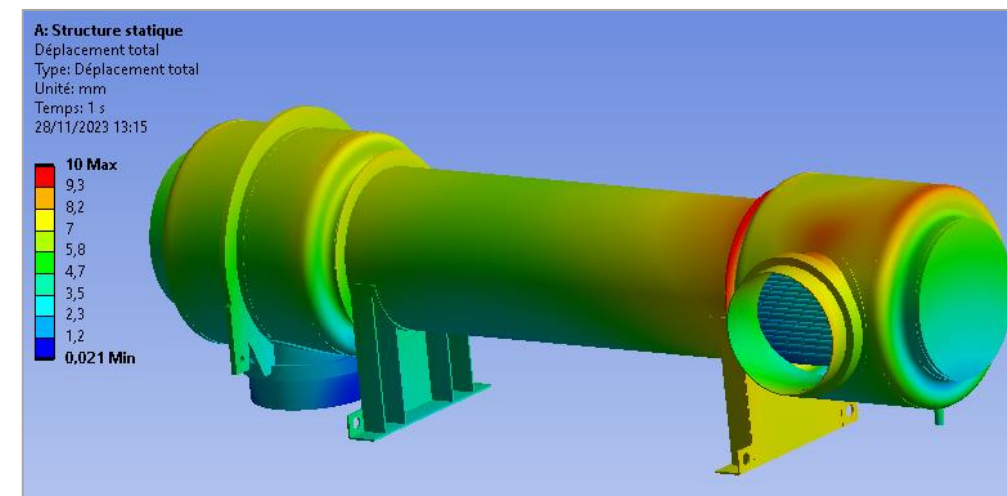
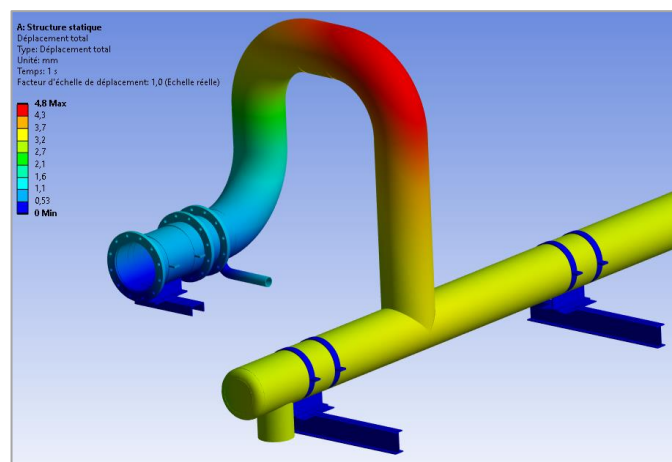
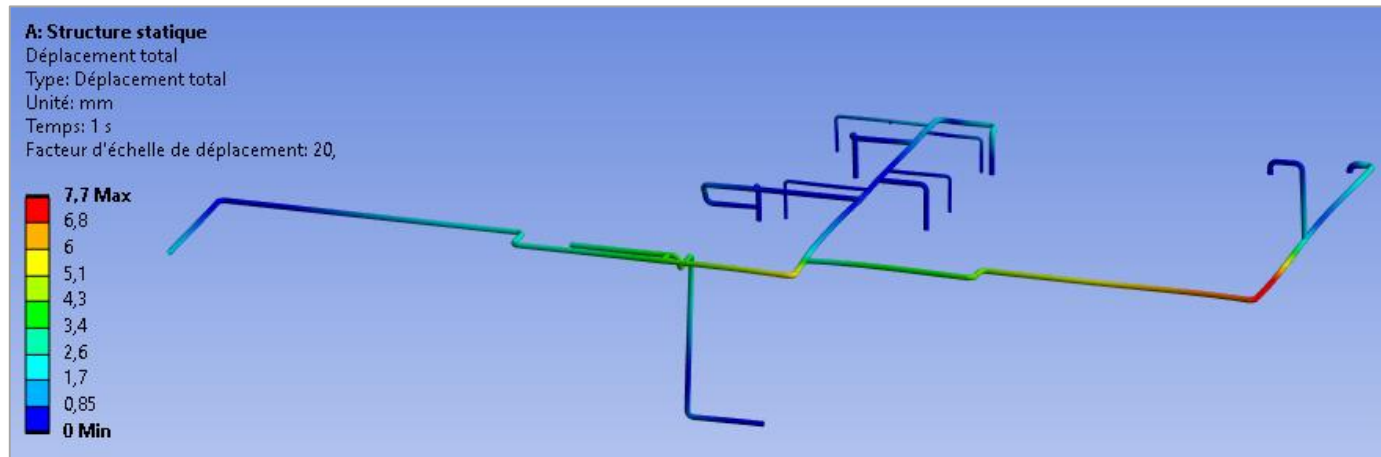
- ▶ Founded in 2013 by Sebastien Besse
- ▶ Industrial design office: our specialty is, but not limited to, steel frames, industrial piping, pressure vessels

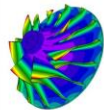
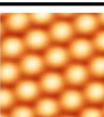
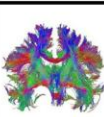


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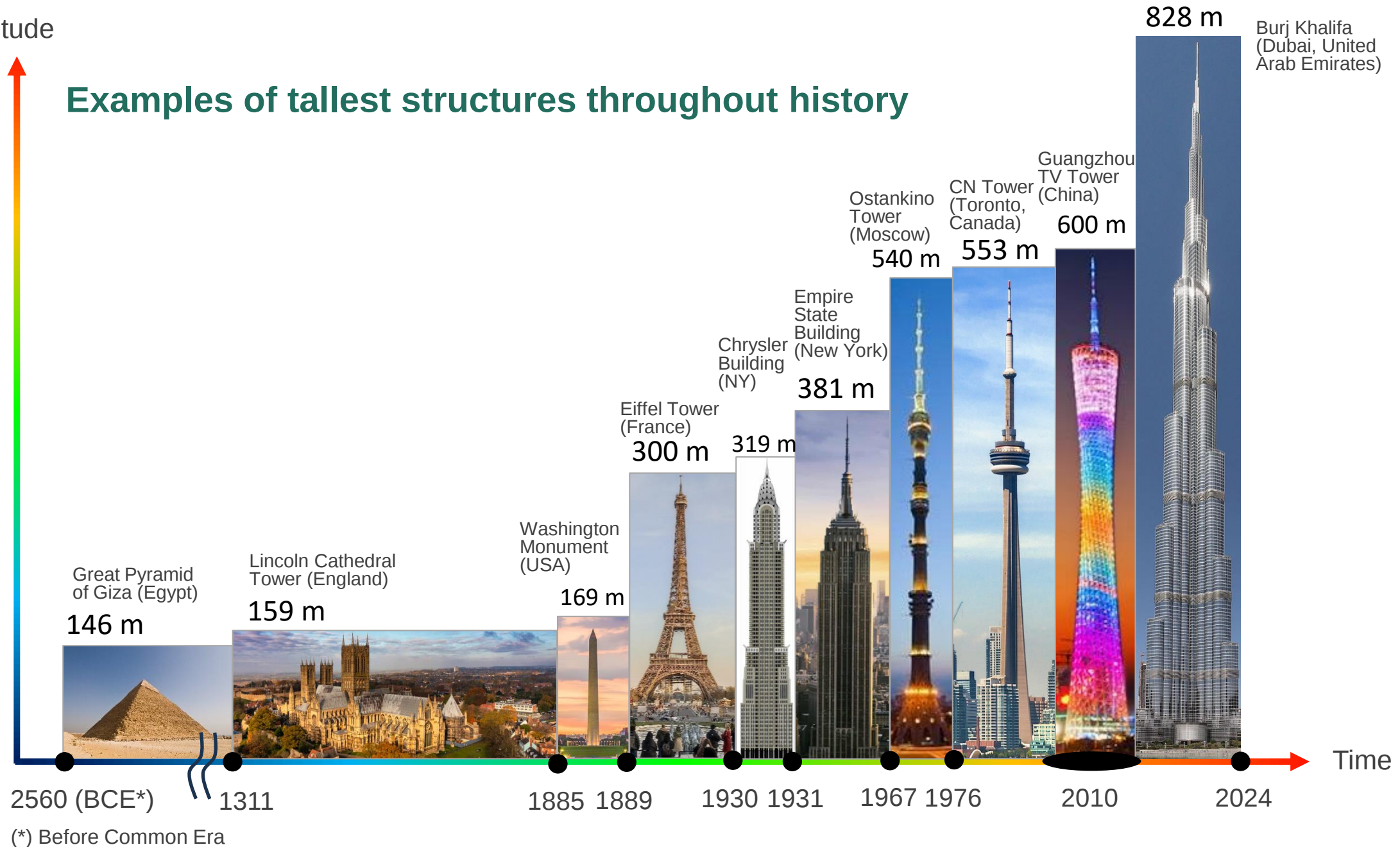
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MECANIQUE DU SOLIDE		$\begin{pmatrix} \sigma_{11} \\ \sigma_{22} \\ \sigma_{33} \\ \sigma_{23} \\ \sigma_{13} \\ \sigma_{12} \end{pmatrix} = \begin{pmatrix} C_{1111} & C_{1122} & C_{1133} & C_{1123} & C_{1113} & C_{1112} \\ C_{2211} & C_{2222} & C_{2233} & C_{2223} & C_{2213} & C_{2212} \\ C_{3311} & C_{3322} & C_{3333} & C_{3323} & C_{3313} & C_{3312} \\ C_{2311} & C_{2322} & C_{2333} & C_{2323} & C_{2313} & C_{2312} \\ C_{1311} & C_{1322} & C_{1333} & C_{1323} & C_{1313} & C_{1312} \\ C_{1211} & C_{1222} & C_{1233} & C_{1223} & C_{1213} & C_{1212} \end{pmatrix} \begin{pmatrix} \epsilon_{11} \\ \epsilon_{22} \\ \epsilon_{33} \\ \epsilon_{23} \\ \epsilon_{13} \\ \epsilon_{12} \end{pmatrix}$ $\rho \frac{d\vec{v}}{dt} = \rho \sum_i \vec{f}_i + \text{div}(\underline{\sigma})$ $\begin{cases} \frac{d\vec{p}}{dt} = \sum_i \vec{F}_i \\ \vec{\delta}_a = \sum_i M_A(\vec{F}_i) \end{cases}$	 Isaac Newton (1643-1727)  Gustave Eiffel (1832-1923)  Robert Hooke (1635-1703)
MECANIQUE DES FLUIDES		$\frac{\partial \rho \vec{v}}{\partial t} + \text{div}(\rho \vec{v} \otimes \vec{v}) = -\overrightarrow{\text{grad}} p + \text{div} \vec{\tau} + \rho \vec{f}$ $\vec{v}_d = -\frac{k}{\eta} (\overrightarrow{\text{grad}} p - \rho \vec{g})$ $\frac{\partial \rho}{\partial t} + \text{div}(\rho \vec{v}) = 0$	 Henry Darcy (1803-1858)  Georges Gabriel Stokes (1819-1903)  Eugène Péclet (1793-1857)
GRAVITATION		$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R + \Lambda g_{\mu\nu} = \kappa T_{\mu\nu}$ $\overrightarrow{F_{1 \rightarrow 2}} = -G \frac{m_1 m_2}{r^2} \overrightarrow{u_{1 \rightarrow 2}}$ $T = \frac{1}{8\pi k_B} \cdot \frac{\hbar c^3}{GM}$	 Albert Einstein (1879-1955)  Stephen Hawking (1942-)  Isaac Newton (1643-1727)
PHYSIQUE NUCLEAIRE		$E = \gamma \cdot mc^2 = \frac{mc^2}{\sqrt{1 - \frac{v^2}{c^2}}}$ $a_0 = \frac{1}{4\pi\epsilon_0} \cdot \frac{2q_1 q_2}{\mu v^2}$ $N(t) = N_0 \cdot e^{-\lambda t}$	 Dmitri Mendeleev (1834-1907)  Ernest Rutherford (1871-1937)  Pierre et Marie Curie (1859-1906; 1867-1934)
ELECTROMAGNETISME		$\begin{cases} \text{div}(\vec{E}) = \frac{\rho}{\epsilon_0} \\ \overrightarrow{\text{rot}} \vec{E} = -\frac{\partial \vec{B}}{\partial t} \\ \text{div}(\vec{B}) = 0 \\ \overrightarrow{\text{rot}} \vec{B} = \mu_0 \cdot \left(\vec{j} + \epsilon_0 \frac{\partial \vec{E}}{\partial t} \right) \end{cases}$ $\vec{B} = \frac{\mu_0 I}{2\pi r} \vec{e}_\theta$ $P = \frac{dE}{dt}$	 James Clerk Maxwell (1831-1879)  Nikola Tesla (1856-1943)  James Watt (1736-1819)
PHYSIQUE QUANTIQUE		$\frac{\hat{p}}{2m} \psi(t)\rangle + V(\hat{r}, t) \psi(t)\rangle = i\hbar \frac{\partial \psi(t)\rangle}{\partial t}$ $f(x, t) = \frac{1}{\sqrt{2\pi}} \int_{-\infty}^{+\infty} A(k) \cdot e^{i(kx - w(k)t)} dk$ $L_{\Omega, \nu}^{\circ} = \frac{2\hbar \nu^3}{c^2} \cdot \frac{1}{e^{\hbar \nu / k_B T} - 1}$ $E = h\nu$	 Erwin Schrödinger (1887-1961)  Richard Feynman (1918-1988)  Max Planck (1858-1947)
THERMODYNAMIQUE		$W + Q_c + Q_m + Q_f = 0$ $\frac{Q_c}{T_c} + \frac{Q_m}{T_m} + \frac{Q_f}{T_f} = \Delta S$ $\Delta S = \Delta S_{\text{syst}} + \Delta S_{\text{ext}} \geq 0$ $U = W + Q$	 Ludwig Boltzmann (1844-1906)  James Prescott Joule (1818-1889)  Sadi Carnot (1796-1832)
DIFFUSION MOLECULAIRE		$\frac{\partial C}{\partial t} + \text{div}(\vec{j}) = P_+ + P_-$ $\vec{j} = -D \overrightarrow{\text{grad}}(C)$ $D = \frac{k_b T}{6\pi\eta R_h}$	 Adolf Eugène Fick (1829-1901)  Georges Gabriel Stokes (1819-1903)  Albert Einstein (1879-1955)
THERMIQUE		$\rho c \frac{\partial T}{\partial t} + \text{div}(\vec{j}) = P_+ + P_-$ $\vec{j} = -\lambda \overrightarrow{\text{grad}}(T)$ $P = \frac{\delta T}{dt}$	 Joule (1818-1889)  Joseph Fourier (1768-1830)  William Thomson Lord Kelvin (1824-1907)
OPTIQUE		$I(\theta) = I_0 \left(\frac{\sin\left(\frac{N\pi d}{\lambda} \sin(\theta)\right)}{\sin\left(\frac{\pi d}{\lambda} \sin(\theta)\right)} \right)^2$ $\langle P \rangle = \frac{\mu_0}{12\pi c} \cdot \omega^4 p_0^2$ $n_1 \sin(\theta_1) = n_2 \sin(\theta_2)$	 René Descartes (1596-1650)  John William Strutt Rayleigh (1842-1919)  Augustin Fresnel (1788-1827)

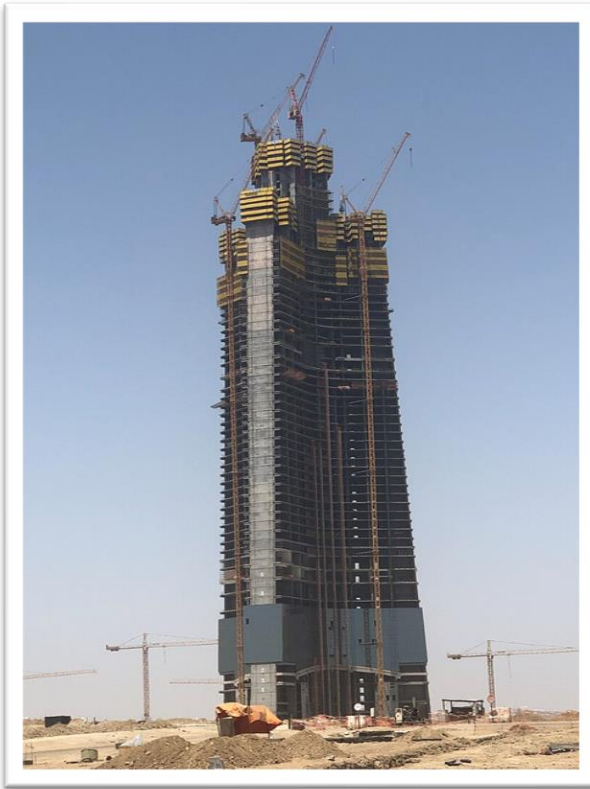
Altitude

Examples of tallest structures throughout history



Examples of on going projects of mega-tall skyscrapers

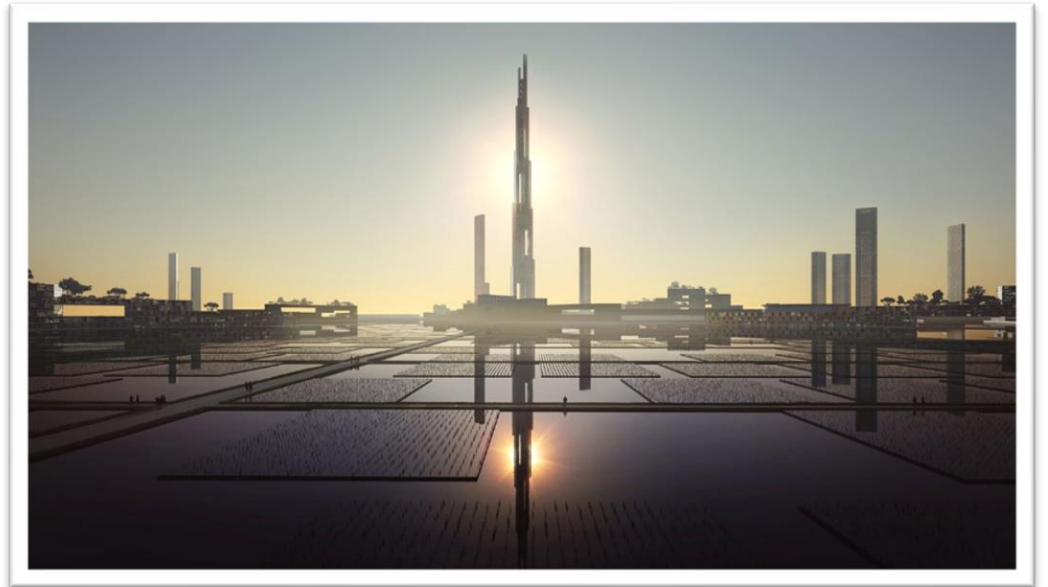
Djeddah Tower 1007 m
(Saudi Arabia)



Oblisco Capitale 1000 m
(Egypt)



Sky Mile Tower 1700 m
Tokyo (Japan)



X-Seed 4000 (Tokyo, 1995)

130 *Journal of Urban Technology*

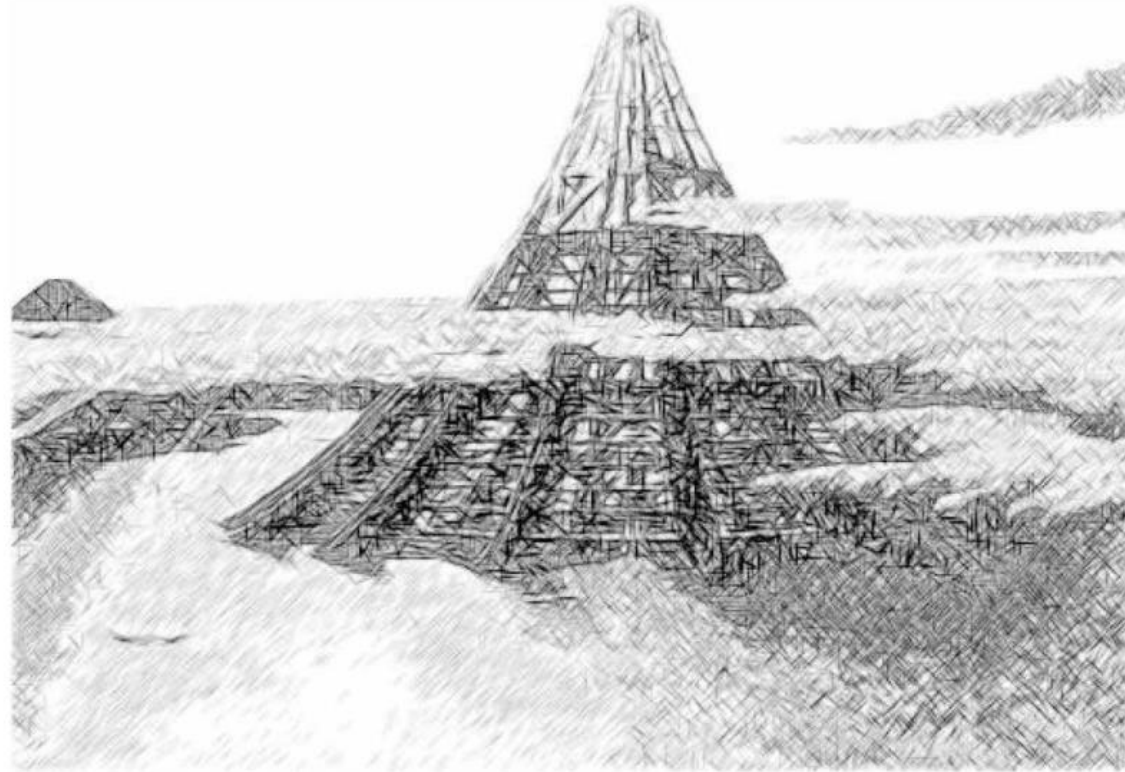
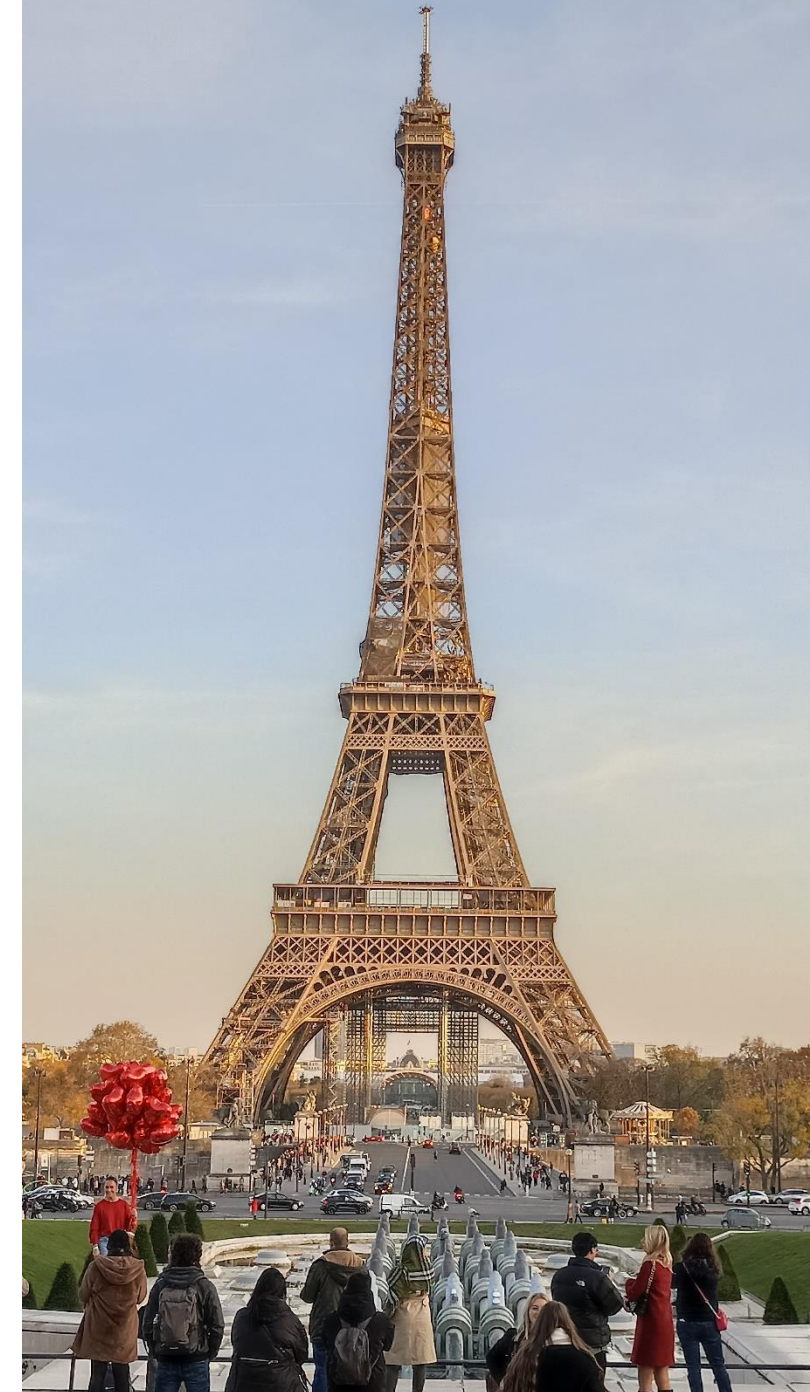
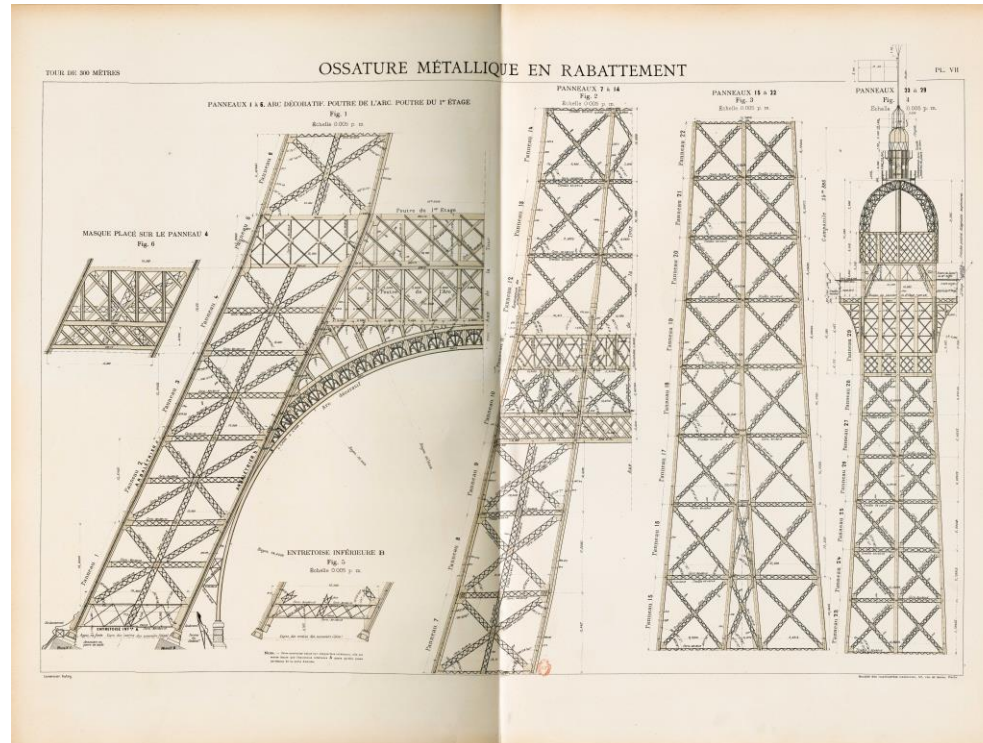
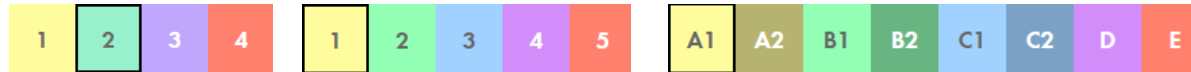


Figure 11. X-seed 4000, proposed by the Taisei Corporation, is a 4 km (2.485miles) height, and 6 km (3.728miles) wide sea-base structure. It contains 800 floors that could accommodate up to one million inhabitants.

Drawing by K. Al-Kodmany

The « prototype » of the Eiffel Tower

- ▶ Built in 1889 with equal angle steel, plates and rivets
- ▶ Designed without electricity or finite element modeling or computers
- ▶ Eurocodes : wind zone 2, seismic zone 1, snow zone A1

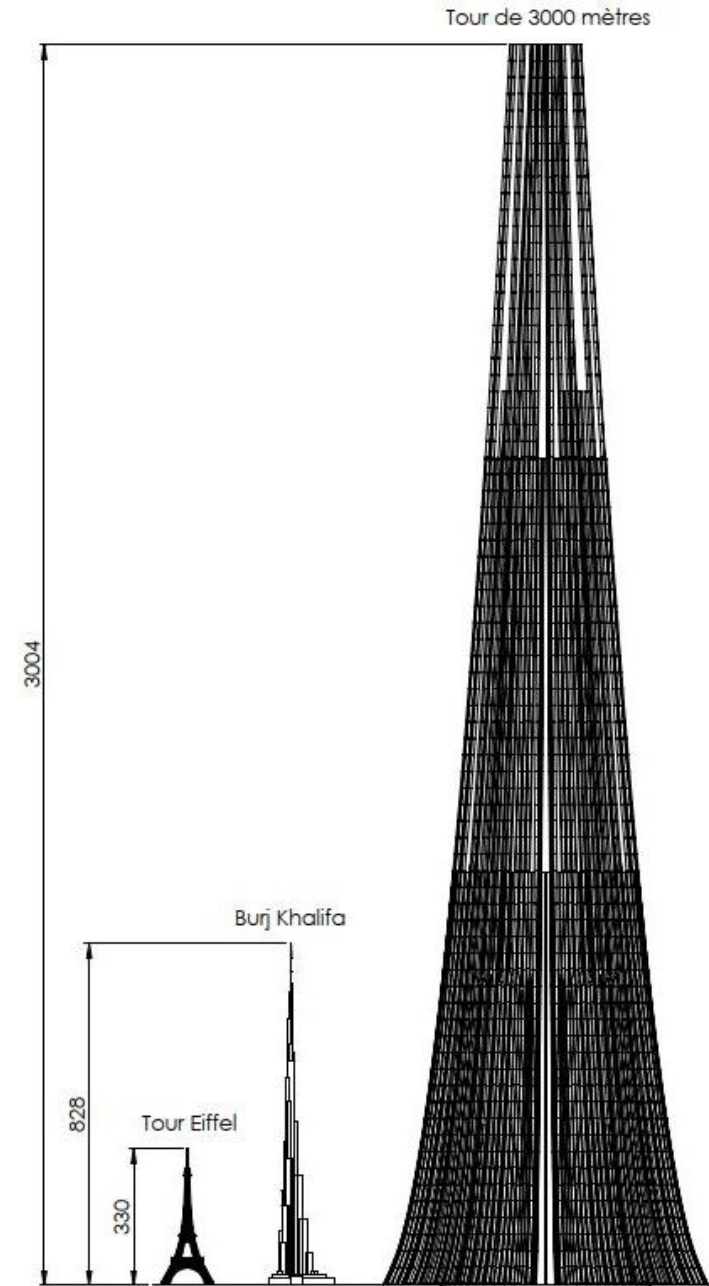


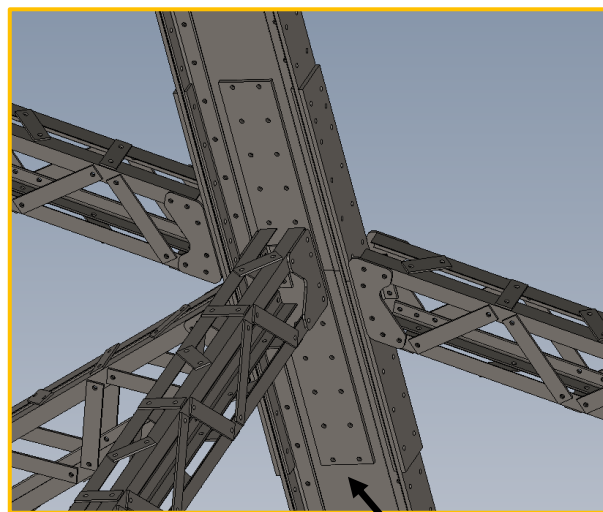
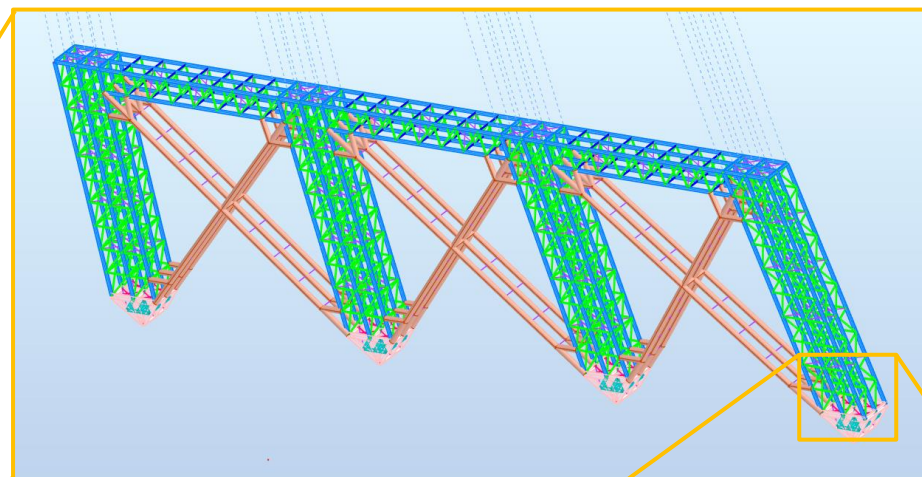
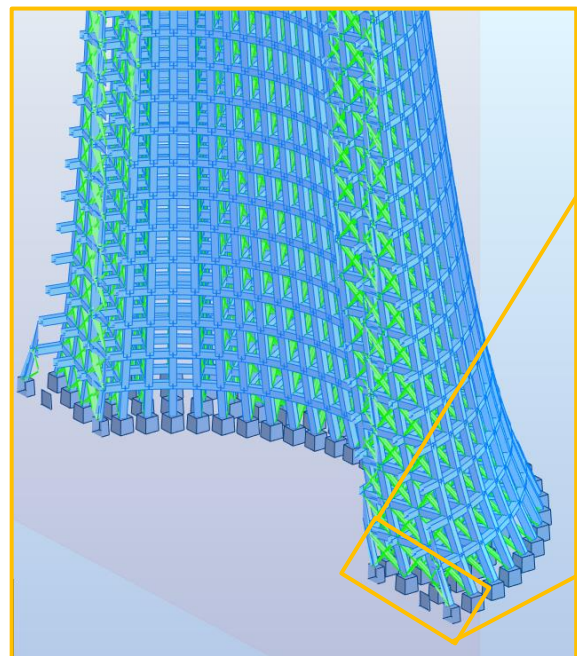
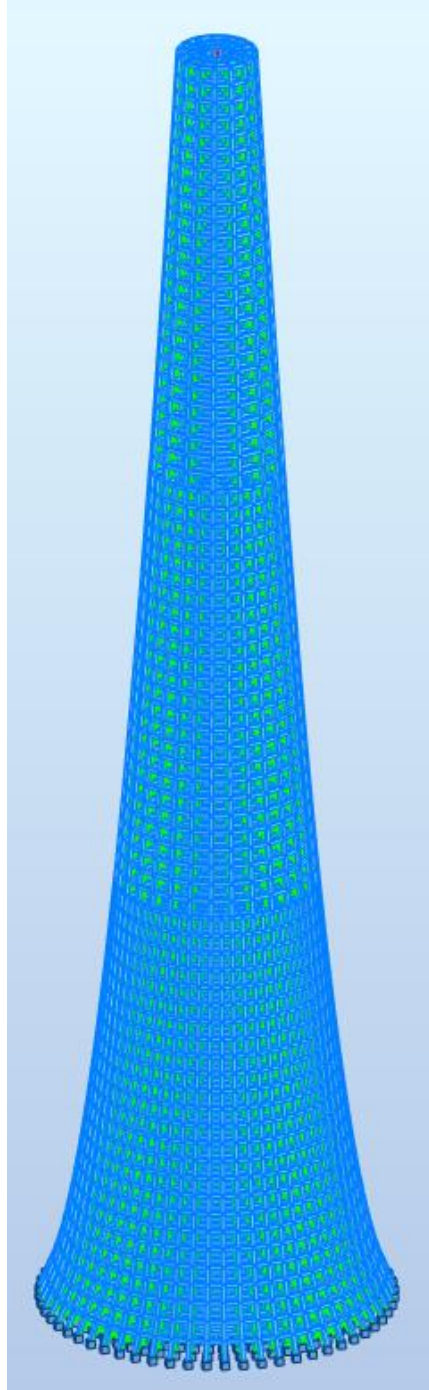
Why a 3000 meter tower is not built in 2024 ?

- ▶ Building a 3000 meter high tower poses many technical challenges, economic, environmental and logistical. Here are some main reasons for which such a structure has never been built.
- ▶ Technical problems and engineering
 - ▶ Structural stability including wind resistance and earthquake resistance
 - ▶ Compressive load on ground columns and risk of buckling
 - ▶ Materials
 - ▶ Elevators
- ▶ Cost
- ▶ Environmental issues
- ▶ Logistics and accessibility
- ▶ Human limits and comfort

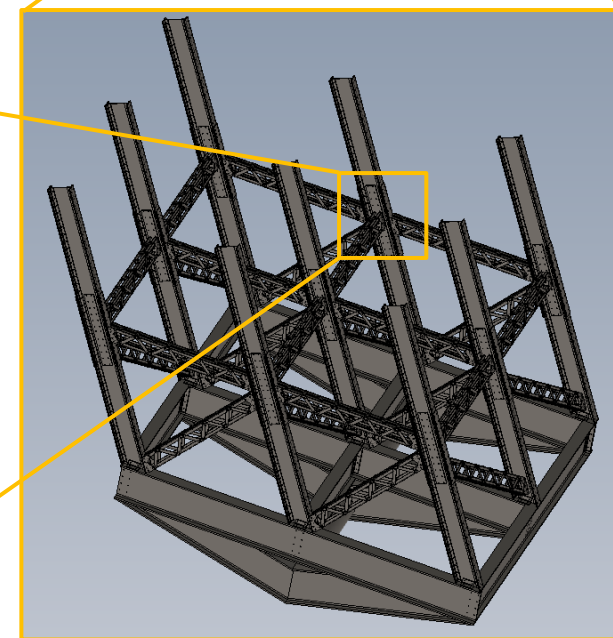
The 3000 meter tower

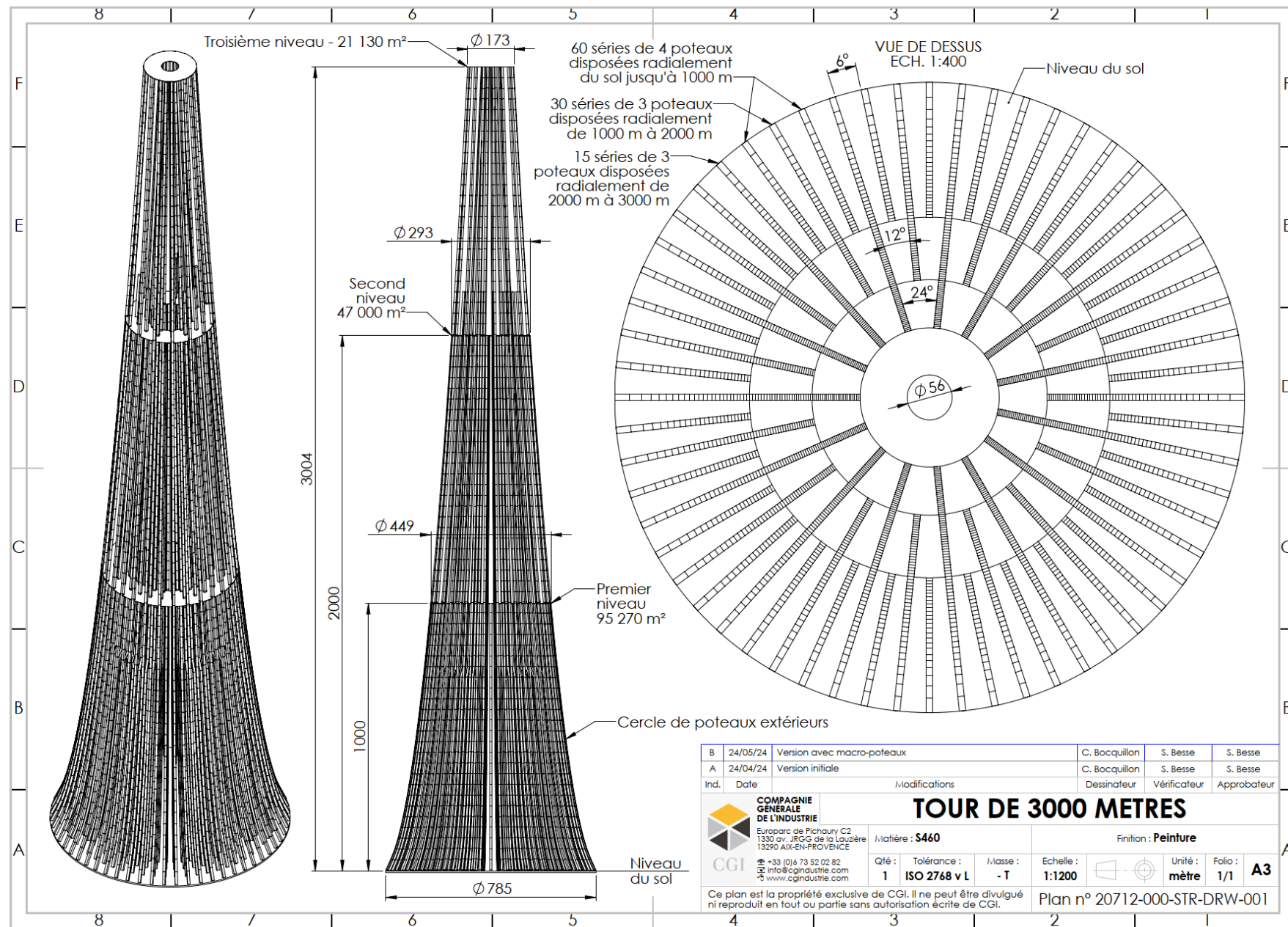
- ▶ Height : 3000 meters
- ▶ Function : commercial center (70%) + tourism (30%)
- ▶ Floors : 4 (ground, 1000, 2000, 3000 meters)
- ▶ Opened structure to reduce wind loads
- ▶ Weight : 750 000 tons (excluding foundations)
- ▶ Material : carbon steel S460
- ▶ Social utility :
 - ▶ Firefighting observation center
 - ▶ Astronomical observatory at 3000 meters
 - ▶ Population gathering area in the event of flooding
 - ▶ Base jump center
 - ▶ Glass floor





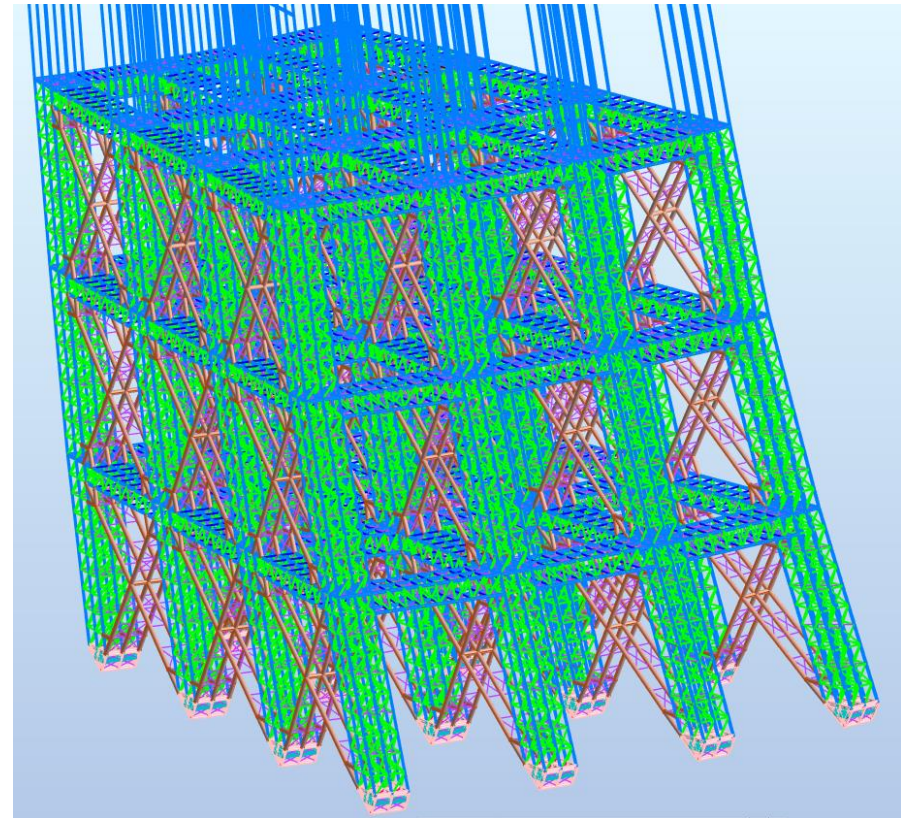
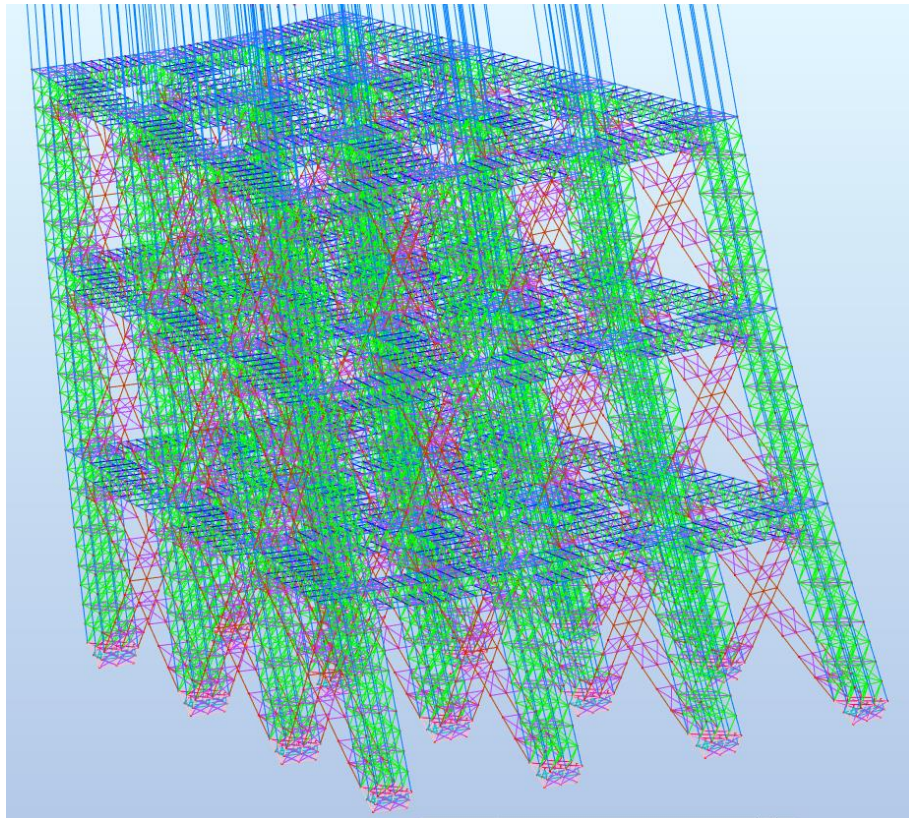
EQUIVALENT TO IPE600





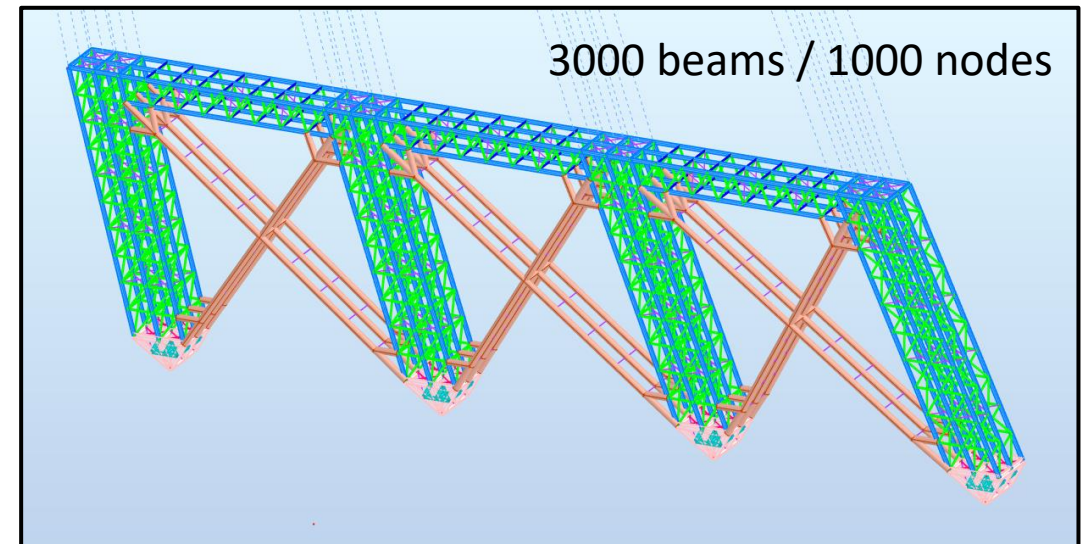
3D view (from 0 to 18°, from z = 0 to 120 m)

- 26 000 beam elements / 12 000 nodes



Software and hardware

- ▶ More than 30 million beams
- ▶ Not suitable for a full 3D realistic model on a computer in 2024 even with 1-D beam elements
- ▶ Calculations performed using the software ANSYS Mechanical 2024 R1 - 4CAD
- ▶ Modeling ground and 1st floor
- ▶ Calculation code : Eurocodes 0, 1, 3, 8
- ▶ Finite element method using ANSYS Mechanical
- ▶ Solve millions of degrees of freedom in seconds
- ▶ Should be justified with linear elasticity and linear material
- ▶ Cylindrical symmetry
- ▶ Buckling length : 1 meter



Method for global design

► Total weight

$$P_{tot} = \alpha P_1 = P_1 \sum_{i=1}^N \prod_{k=0}^{i-1} (1 - t_k)^k$$

$$t_k = \frac{e(z)}{e(z=0)} \times \frac{D_m(z)}{D_m(z=0)}$$

Facteur α

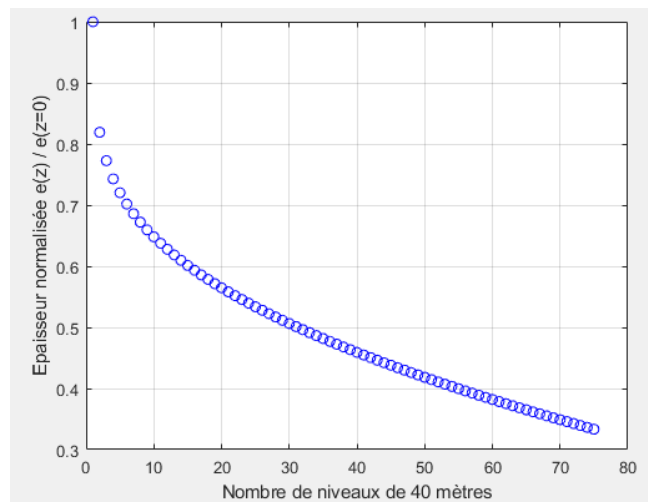
N the number of levels of the tower

P_1 weight of the first level ($z = 0$ to 40 meters)

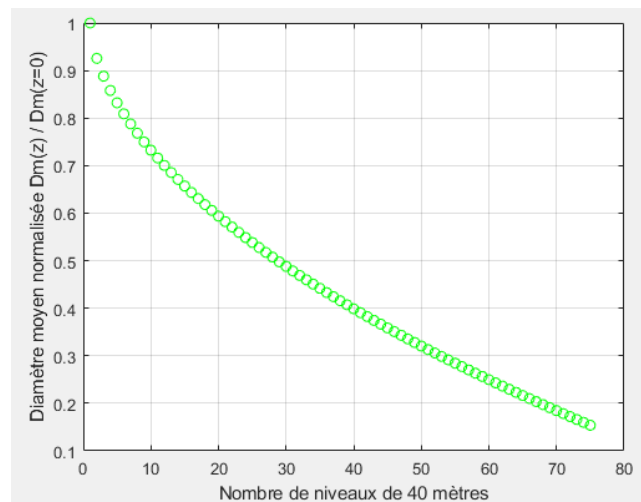
t_k reduction rate from level $k - 1$ to level k

$e(z)$ apparent thickness of the tower along z

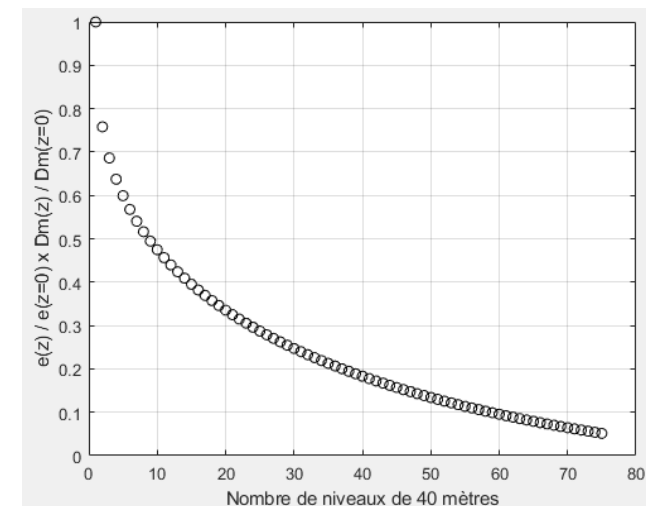
$D_m(z)$ mean diameter of the tower along z



X



=

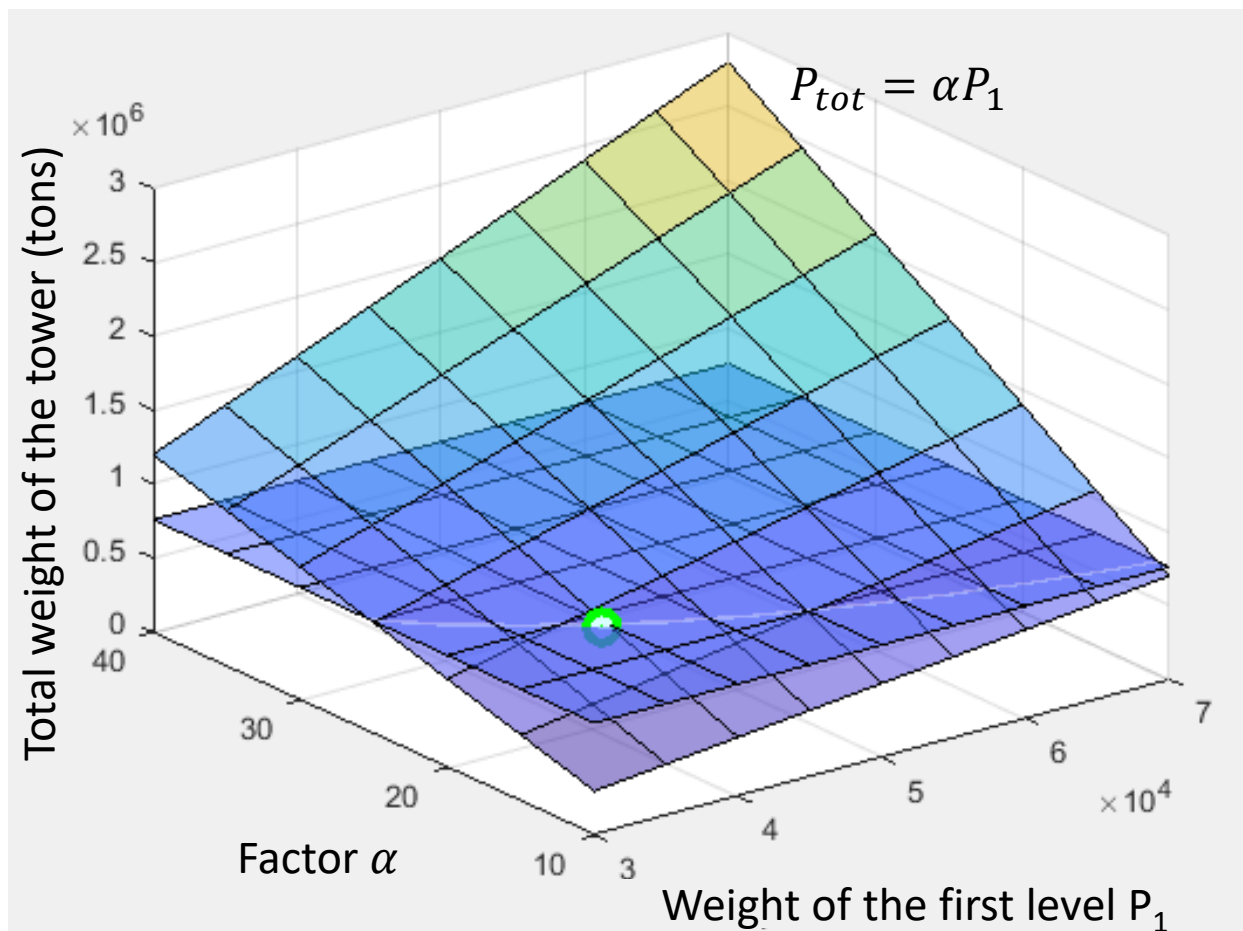


Method for global design

$$P_{tot} < P_1 + 60 \times 4 \times 3000 \text{ tons}$$

- Surface of total weight

$$P_{tot} < 39\,612 \text{ tons} + 60 \times 4 \times 3000 \text{ tons} = 759\,612 \text{ tons}$$



$$(P_1, \alpha, P_{tot}) =$$

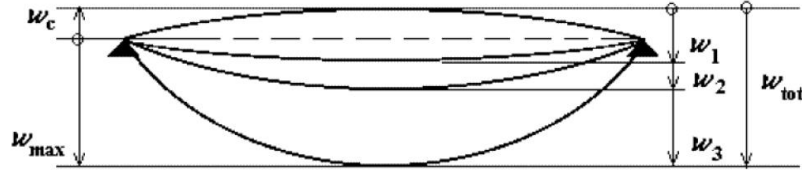
$$(39\,612 \text{ tons}, 18.866, 747\,320 \text{ tons})$$

Ultimate Limit State (ULS)

- Steel S460
- Maximal ratio : 99 %
- Maximal stress : 454 MPa
(< 460 MPa)

Pièce	Profil	Matériau	Lay	Laz	Ratio	Cas
479	OK IPE 600	S 460 M	2.06	10.73	0.99	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
529	OK IPE 600	S 460 M	2.06	10.73	0.99	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
321	OK IPE 600	S 460 M	2.06	10.73	0.98	110 ACC:SEV4=1*1.00 + 2*0.30 + 8*1.00
519	OK IPE 600	S 460 M	2.06	10.73	0.97	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
550	OK IPE 600	S 460 M	2.06	10.73	0.95	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
410	OK IPE 600	S 460 M	2.06	10.73	0.95	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
509	OK IPE 600	S 460 M	2.06	10.73	0.93	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
311	OK IPE 600	S 460 M	2.06	10.73	0.93	110 ACC:SEV4=1*1.00 + 2*0.30 + 8*1.00
272	OK IPE 600	S 460 M	2.06	10.73	0.92	47 ELU/21=1*1.35 + 2*1.05 + 5*1.50
301	OK IPE 600	S 460 M	2.06	10.73	0.91	110 ACC:SEV4=1*1.00 + 2*0.30 + 8*1.00
551	OK IPE 600	S 460 M	2.06	10.73	0.90	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
282	OK IPE 600	S 460 M	2.06	10.73	0.90	47 ELU/21=1*1.35 + 2*1.05 + 5*1.50
400	OK IPE 600	S 460 M	2.06	10.73	0.89	110 ACC:SEV4=1*1.00 + 2*0.30 + 8*1.00
262	OK IPE 600	S 460 M	2.06	10.73	0.89	47 ELU/21=1*1.35 + 2*1.05 + 5*1.50
390	OK IPE 600	S 460 M	2.06	10.73	0.88	110 ACC:SEV4=1*1.00 + 2*0.30 + 8*1.00
548	OK IPE 600	S 460 M	2.06	10.73	0.87	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
558	OK IPE 600	S 460 M	2.06	10.73	0.87	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
539	OK IPE 600	S 460 M	2.06	10.73	0.86	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
461	OK IPE 600	S 460 M	2.06	10.73	0.84	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
552	OK IPE 600	S 460 M	2.06	10.73	0.84	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
9	OK IPE 600	S 460 M	2.06	10.73	0.83	51 ELU/25=1*1.35 + 2*1.05 + 6*1.50
273	OK IPE 600	S 460 M	2.06	10.73	0.82	110 ACC:SEV4=1*1.00 + 2*0.30 + 8*1.00
553	OK IPE 600	S 460 M	2.06	10.73	0.81	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
372	OK IPE 600	S 460 M	2.06	10.73	0.81	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
263	OK IPE 600	S 460 M	2.06	10.73	0.80	47 ELU/21=1*1.35 + 2*1.05 + 5*1.50
540	OK IPE 600	S 460 M	2.06	10.73	0.80	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
520	OK IPE 600	S 460 M	2.06	10.73	0.79	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
541	OK IPE 600	S 460 M	2.06	10.73	0.78	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
521	OK IPE 600	S 460 M	2.06	10.73	0.77	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
274	OK IPE 600	S 460 M	2.06	10.73	0.77	110 ACC:SEV4=1*1.00 + 2*0.30 + 8*1.00
554	OK IPE 600	S 460 M	2.06	10.73	0.76	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
542	OK IPE 600	S 460 M	2.06	10.73	0.76	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
469	OK IPE 600	S 460 M	2.06	10.73	0.76	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
522	OK IPE 600	S 460 M	2.06	10.73	0.76	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
528	OK IPE 600	S 460 M	2.06	10.73	0.75	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
283	OK IPE 600	S 460 M	2.06	10.73	0.75	51 ELU/25=1*1.35 + 2*1.05 + 6*1.50
264	OK IPE 600	S 460 M	2.06	10.73	0.75	110 ACC:SEV4=1*1.00 + 2*0.30 + 8*1.00
380	OK IPE 600	S 460 M	2.06	10.73	0.75	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
842 Poutre st	OK IPE 200	S 460 M	48.43	178.90	0.74	51 ELU/25=1*1.35 + 2*1.05 + 6*1.50
543	OK IPE 600	S 460 M	2.06	10.73	0.74	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
265	OK IPE 600	S 460 M	2.06	10.73	0.74	47 ELU/21=1*1.35 + 2*1.05 + 5*1.50
987 Poutre st	OK IPE 200	S 460 M	48.43	178.90	0.74	47 ELU/21=1*1.35 + 2*1.05 + 5*1.50
518	OK IPE 600	S 460 M	2.06	10.73	0.74	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
547	OK IPE 600	S 460 M	2.06	10.73	0.74	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
523	OK IPE 600	S 460 M	2.06	10.73	0.74	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50
557	OK IPE 600	S 460 M	2.06	10.73	0.74	39 ELU/13=1*1.35 + 2*1.05 + 3*1.50

Serviceability Limit State (SLS)



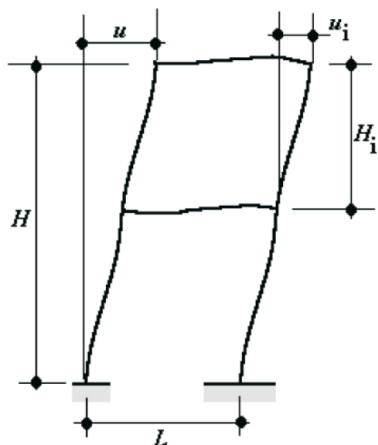
Légende

- w_c Contreflèche dans l'élément structural non chargé
- w_1 Partie initiale de la flèche sous les charges permanentes de la combinaison d'actions correspondante selon les expressions (6.14a) à (6.16b).
- w_2 Partie à long terme de la flèche sous les charges permanentes.
- w_3 Partie additionnelle de la flèche due aux actions variables de la combinaison d'actions correspondante d'après les expressions (6.14a) à (6.16b).
- w_{tot} Flèche totale, soit somme de w_1 , w_2 , w_3 .
- w_{max} Flèche résiduelle totale compte tenu de la contreflèche.

Pièce	Profil	Matériau	Ratio(uy)	Cas (uy)	Ratio(uz)	Cas (uz)
1045	OK IPE 600	S 460 M	0.31	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
1024	OK IPE 600	S 460 M	0.31	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.00	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
1038	OK IPE 600	S 460 M	0.30	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
865	OK IPE 600	S 460 M	0.30	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
899	OK IPE 600	S 460 M	0.29	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
885	OK IPE 600	S 460 M	0.29	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
757	OK IPE 600	S 460 M	0.28	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00	0.00	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
741	OK IPE 600	S 460 M	0.28	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00	0.01	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
1050	OK IPE 600	S 460 M	0.28	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	61 ELS:CAR/7=1*1.00 + 2*0.70 + 3*1.00
1029	OK IPE 600	S 460 M	0.27	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	61 ELS:CAR/7=1*1.00 + 2*0.70 + 3*1.00
749	OK IPE 600	S 460 M	0.27	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00	0.01	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
1043	OK IPE 600	S 460 M	0.27	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	61 ELS:CAR/7=1*1.00 + 2*0.70 + 3*1.00
870	OK IPE 600	S 460 M	0.26	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
904	OK IPE 600	S 460 M	0.26	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.02	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
890	OK IPE 600	S 460 M	0.26	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.02	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
746	OK IPE 600	S 460 M	0.25	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.02	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
762	OK IPE 600	S 460 M	0.25	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00	0.01	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00
1033	OK IPE 600	S 460 M	0.25	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00	0.00	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
999	OK IPE 600	S 460 M	0.25	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00	0.00	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00
12047 Poutre stab IPE200_12047	OK IPE 200	S 460 M	0.25	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00	0.04	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00
12046 Poutre stab IPE200_12046	OK IPE 200	S 460 M	0.25	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00	0.05	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00

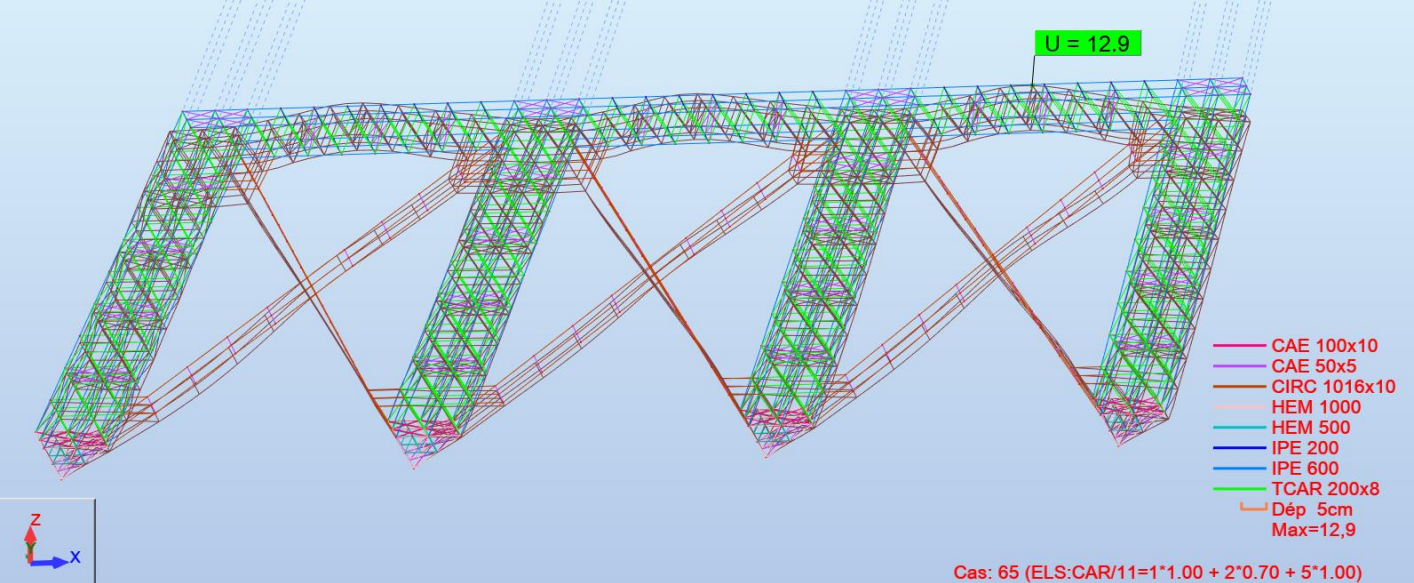
Serviceability Limit State (SLS)

130 mm



Légende

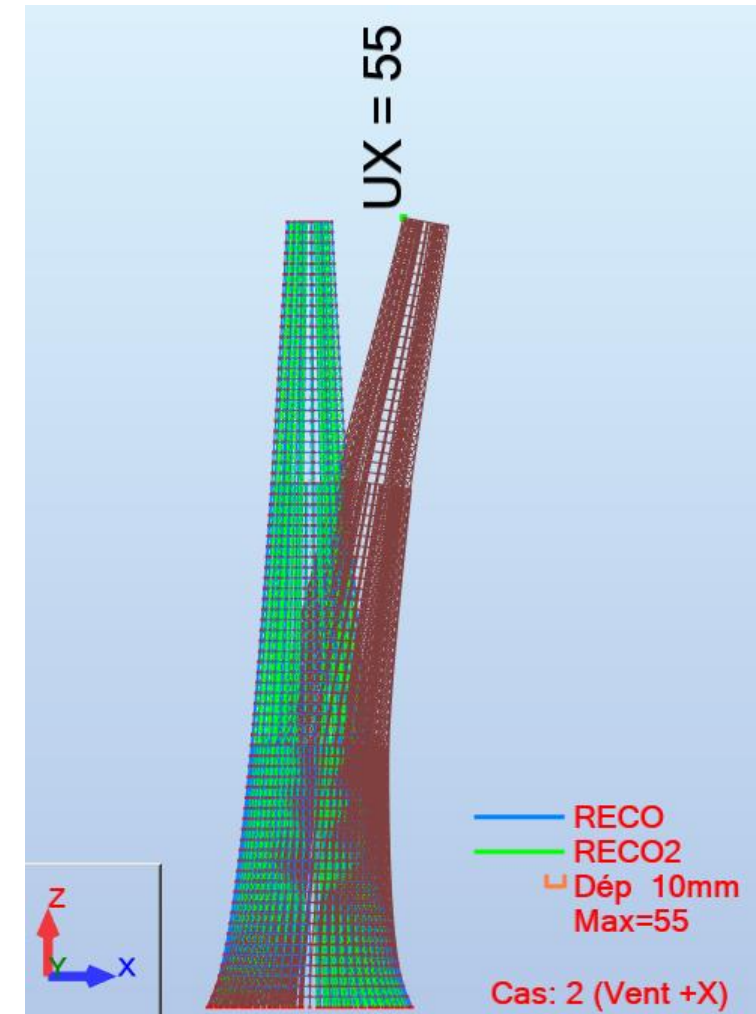
- u Déplacement horizontal général sur la hauteur H du bâtiment
- u_i Déplacement horizontal sur la hauteur H_i d'un étage



Pièce	Profil	Matériau	Ratio(vx)	Cas (vx)	Ratio(vy)▲	Cas (vy)
267	OK IPE 600	S 460 M	0.07	61 ELS:CAR/7=1*1.00 + 2*0.70 + 3*1.00	0.18	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
232	OK IPE 600	S 460 M	0.11	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00	0.17	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
282	OK IPE 600	S 460 M	0.14	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00	0.17	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
272	OK IPE 600	S 460 M	0.14	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00	0.17	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
209	OK IPE 600	S 460 M	0.05	61 ELS:CAR/7=1*1.00 + 2*0.70 + 3*1.00	0.16	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
219	OK IPE 600	S 460 M	0.06	61 ELS:CAR/7=1*1.00 + 2*0.70 + 3*1.00	0.16	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
273	OK IPE 600	S 460 M	0.11	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00	0.16	67 ELS:CAR/13=1*1.00 + 2*0.70 + 6*1.00
277	OK IPE 600	S 460 M	0.07	61 ELS:CAR/7=1*1.00 + 2*0.70 + 3*1.00	0.15	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
242	OK IPE 600	S 460 M	0.11	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00	0.15	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
229	OK IPE 600	S 460 M	0.07	61 ELS:CAR/7=1*1.00 + 2*0.70 + 3*1.00	0.15	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
222	OK IPE 600	S 460 M	0.09	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00	0.15	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
234	OK IPE 600	S 460 M	0.09	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00	0.15	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00
212	OK IPE 600	S 460 M	0.10	63 ELS:CAR/9=1*1.00 + 2*0.70 + 4*1.00	0.14	65 ELS:CAR/11=1*1.00 + 2*0.70 + 5*1.00

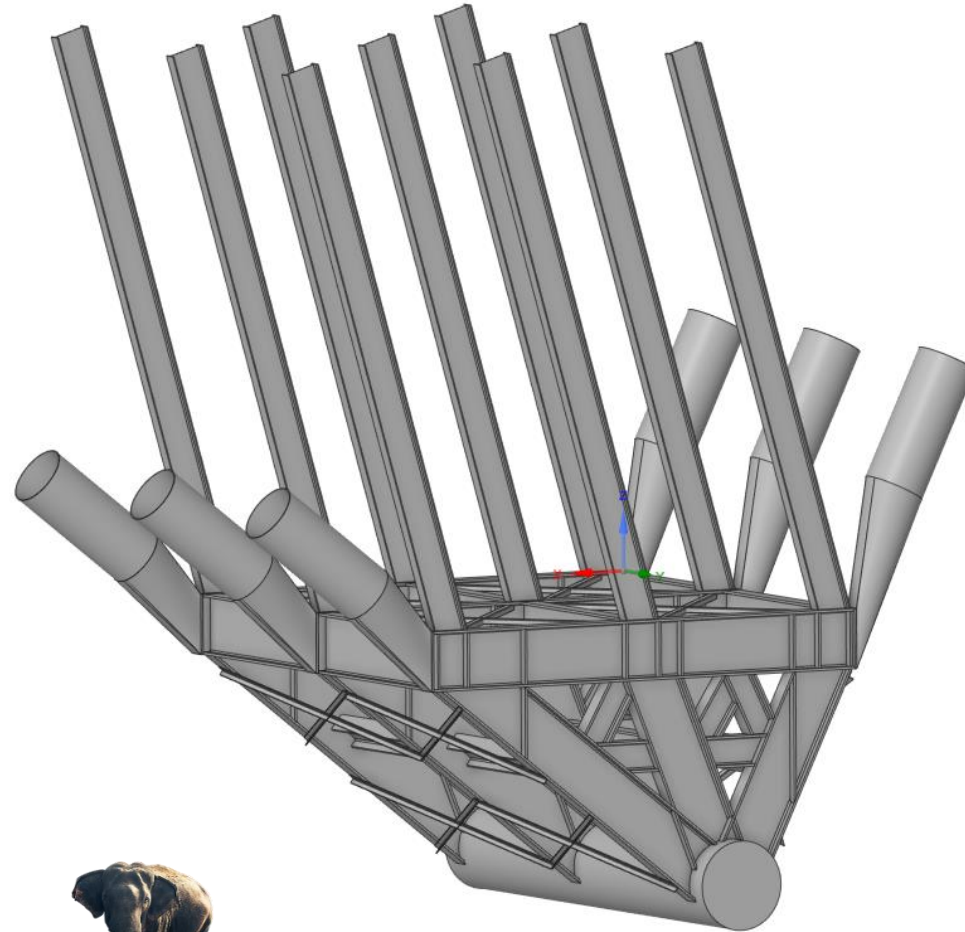
Horizontal wind deflection at $z = 3000$ m

- ▶ Wind deflection based on 300 daN/m^2
- ▶ For Eiffel Tower, Eurocode : $H / 150$
 - ▶ $H / 150 = 300\,000 \text{ mm} / 150 = 2 \text{ meters}$
 - ▶ Experimental : max 130 mm (storm, 1999)
 - ▶ Eiffel tower respects a criteria $H / 2300$
- ▶ The Tower respects a criteria $H / 54\,000$

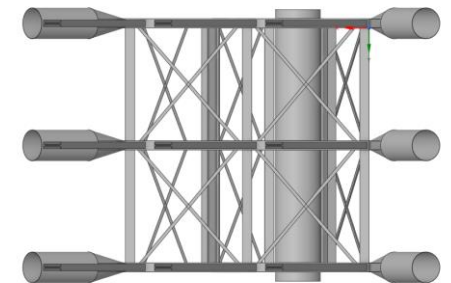
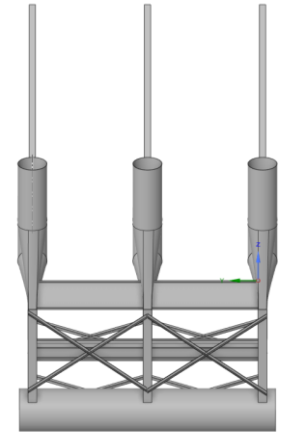
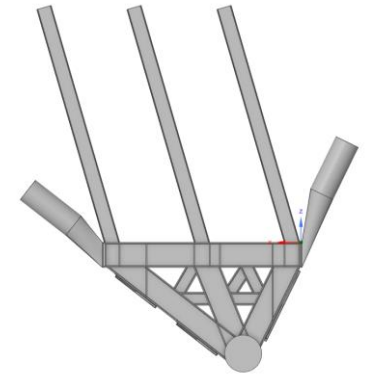


Hinged support (160 tons x 240 supports)

- ▶ IPE600
- ▶ HEM 1000
- ▶ HEM 500
- ▶ CAE 100x10
- ▶ BAR 1500
- ▶ DN1000
- ▶ Steel S460

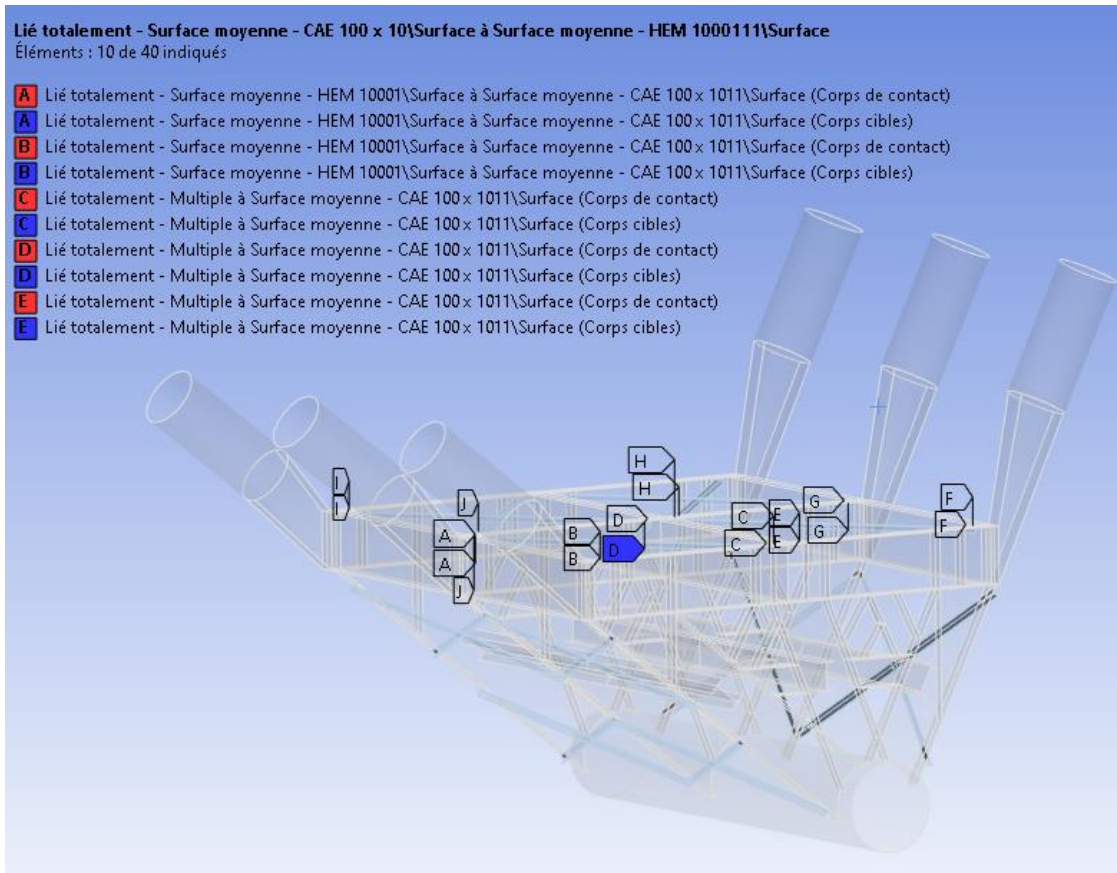


(tonnage of all the supports $\approx$ 6500 elephants)



Hinged support

40 contacts from welded CAE 100 x 10



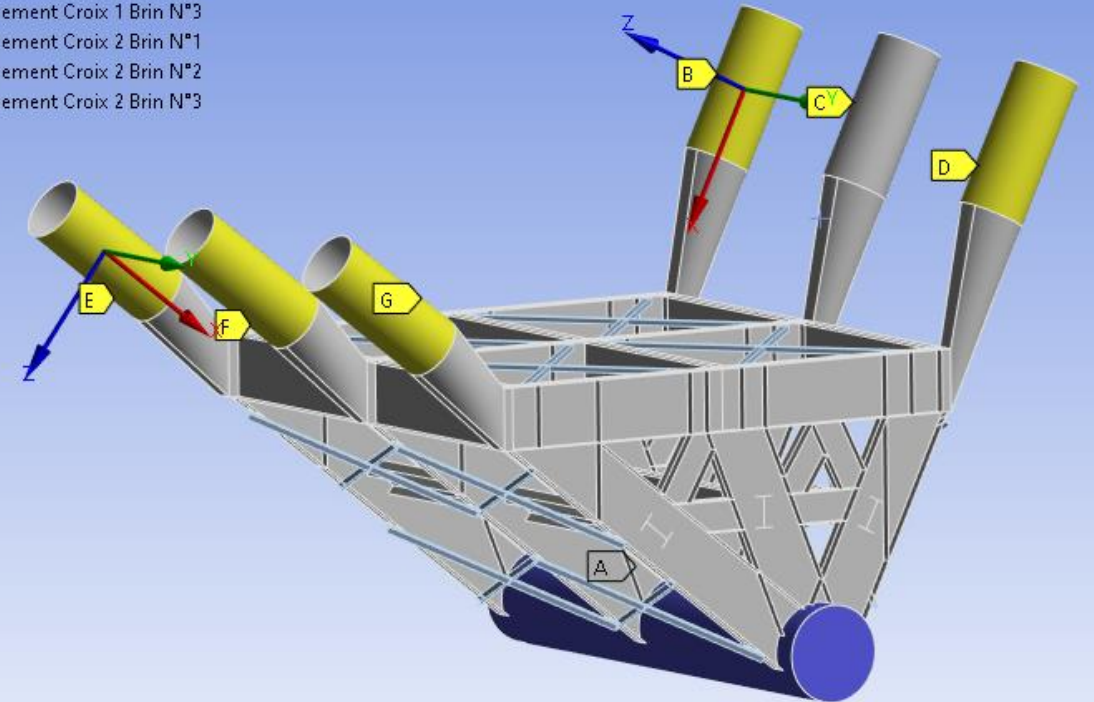
Boundary conditions

A: Structure statique

Déplacement Croix 2 Brin N°3

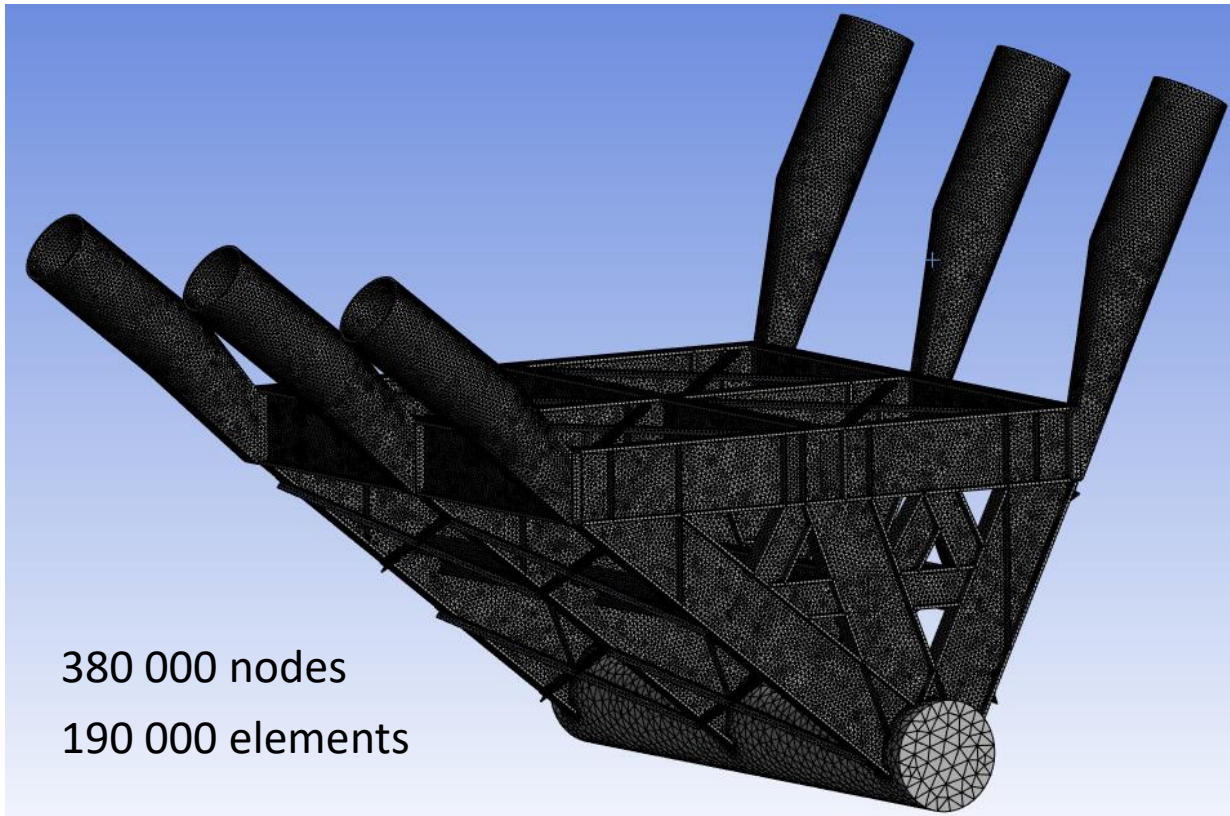
Temps: 1, s

- A** Support fixe
- B** Déplacement Croix 1 Brin N°1
- C** Déplacement Croix 1 Brin N°2
- D** Déplacement Croix 1 Brin N°3
- E** Déplacement Croix 2 Brin N°1
- F** Déplacement Croix 2 Brin N°2
- G** Déplacement Croix 2 Brin N°3



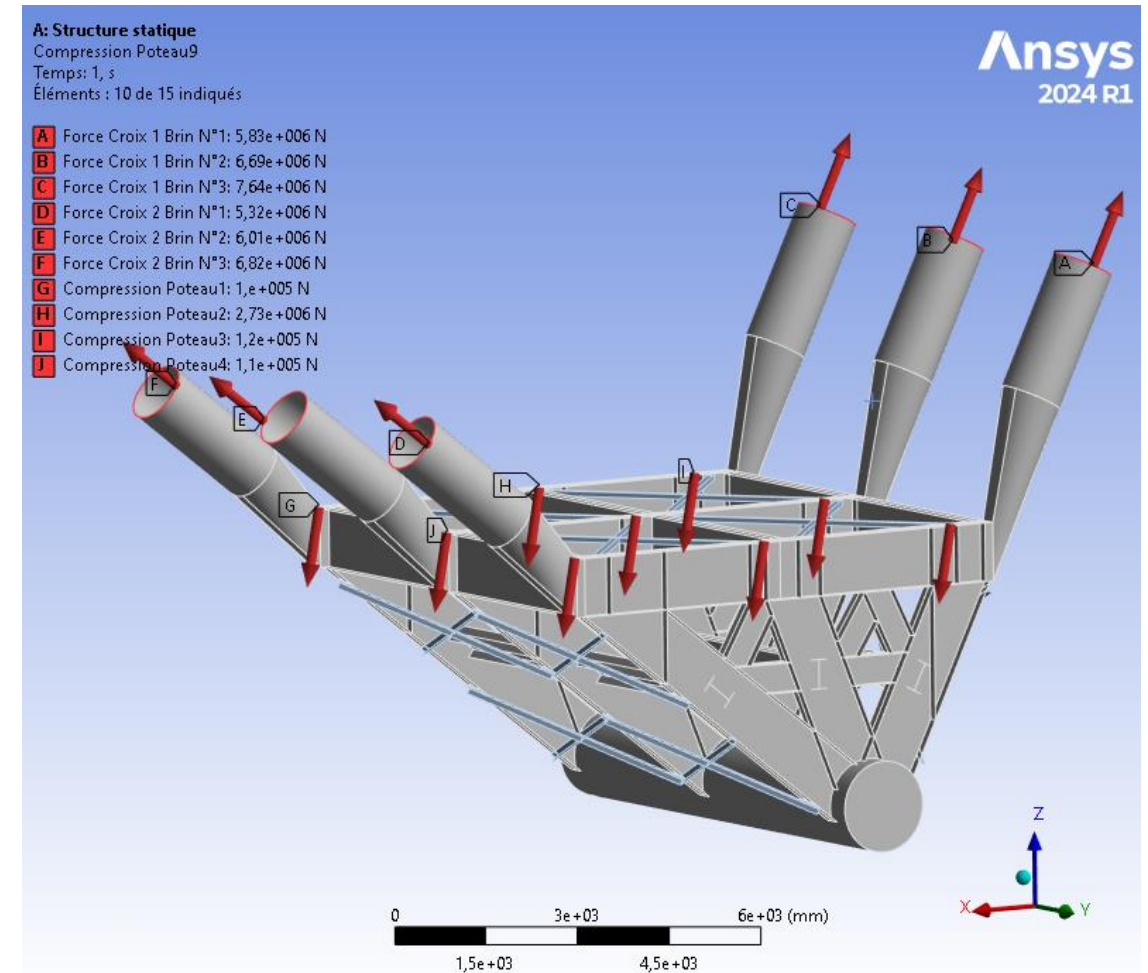
Hinged support

Mesh (triangular quadratic mesh SHELL281)



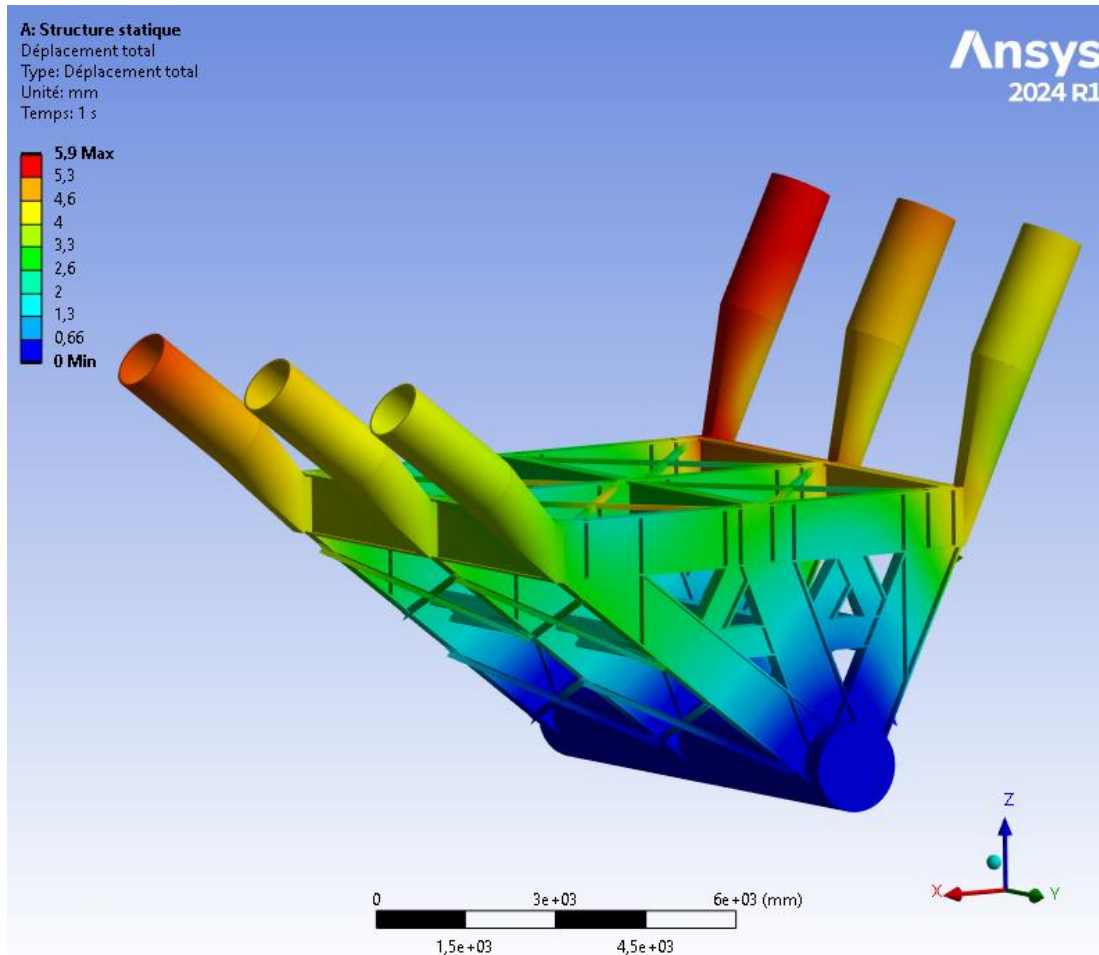
380 000 nodes
190 000 elements

Loads coming from the 3D beam model



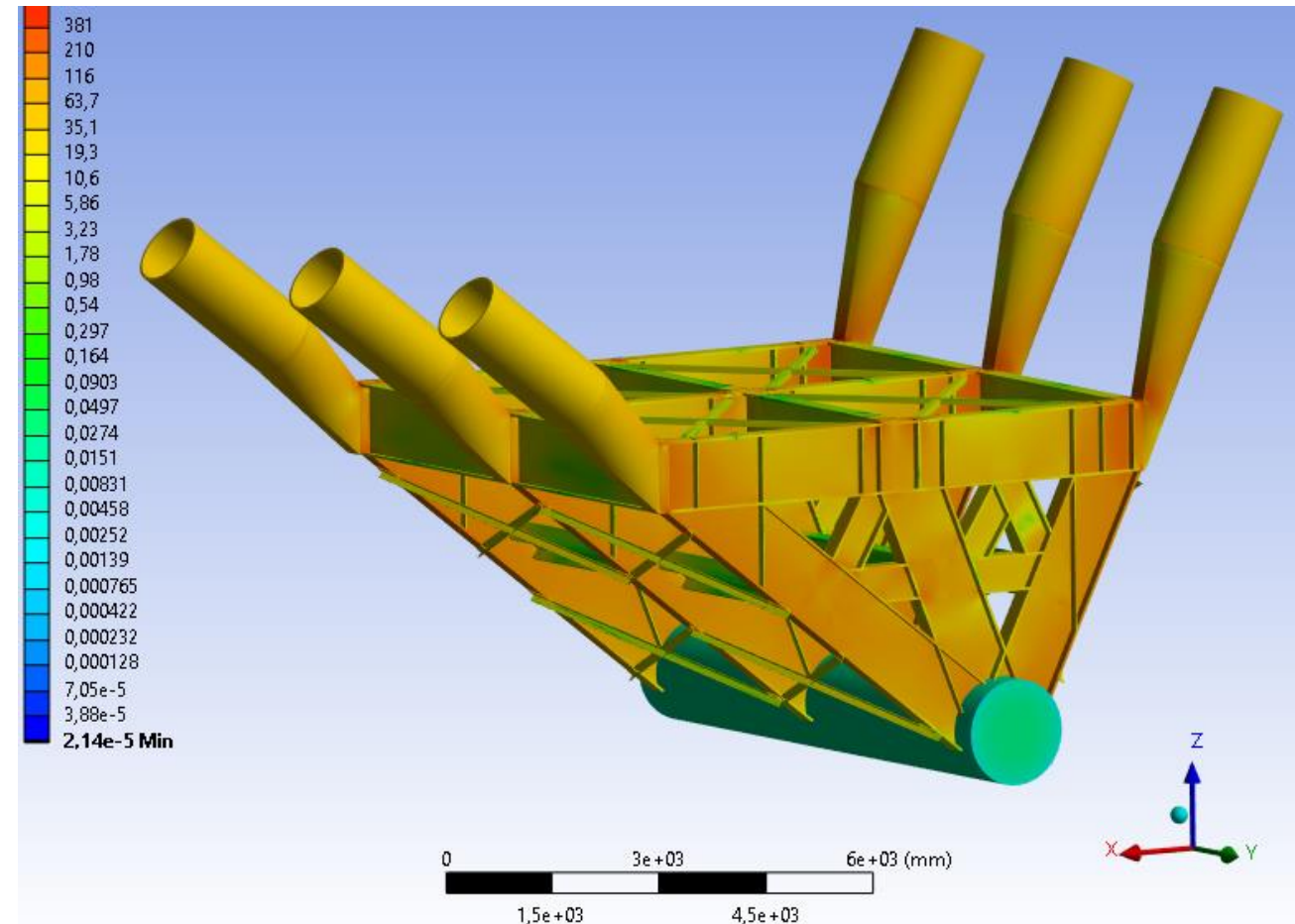
Hinged support

Total displacement



Von Mises stress (nodal values without averages)

Logarithmic scale



Modal analysis and Response Spectrum Method (RSM)

- ▶ Mode superposition method
- ▶ 15 modes
- ▶ Combination of modal response including Complete Quadratic Combination (CQC) method

$$R = \sqrt{\sum_{i=1}^N \sum_{j=1}^N \left(R_i R_j \frac{(\omega_i + \omega_j)^2 \xi^2}{(\omega_i - \omega_j)^2 + (\omega_i + \omega_j)^2 \xi^2} \right)}$$

ξ constant damping ratio

- ▶ Missing mass correction : force due to missing mass

$$F = M \left\{ \{1\} - \sum_{i=1}^m \Gamma_i \{\phi_i\} \right\} S_{A \max}$$

M total mass

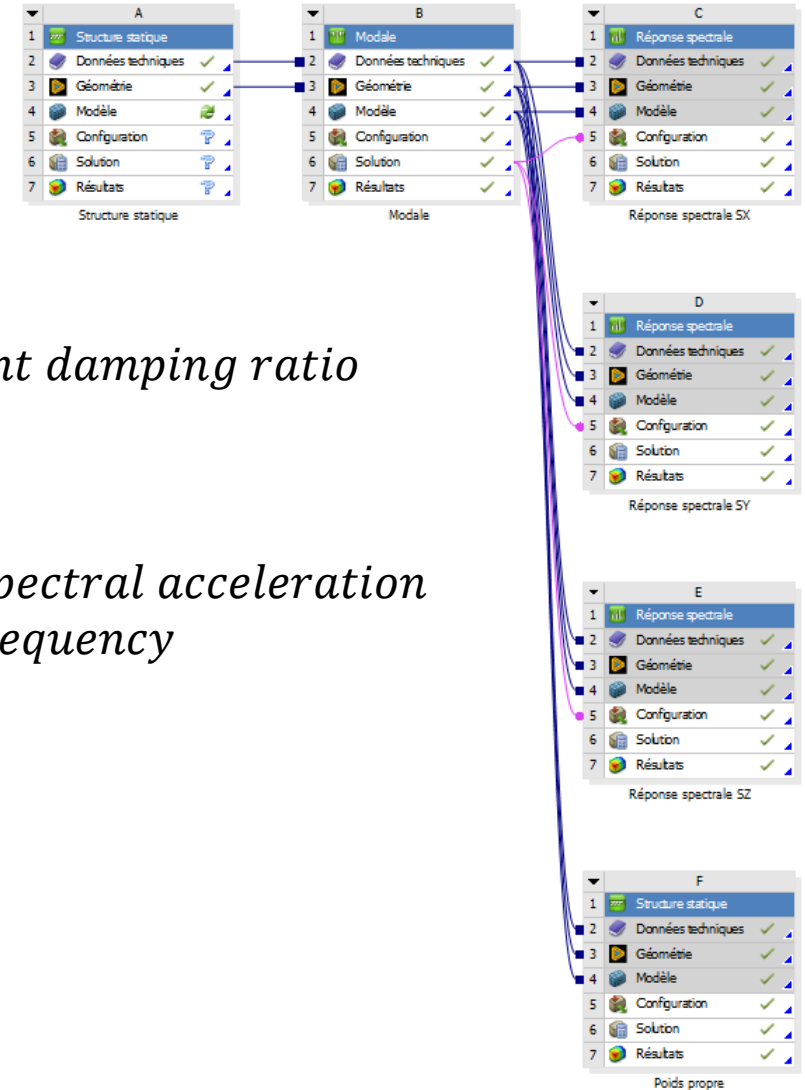
$S_{A \max}$ highest spectral acceleration at the cutoff frequency

- ▶ Spatial combination (triaxial dynamic response)
 - ▶ Maximum response due to earthquake will be highest of three as given :

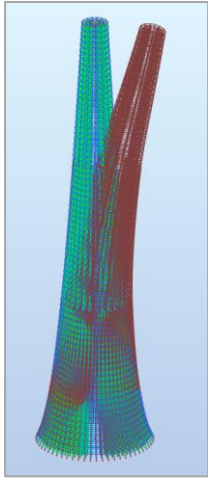
$$R = \pm R_x \pm 0.4 R_y \pm 0.4 R_z$$

$$R = \pm R_y \pm 0.4 R_z \pm 0.4 R_x$$

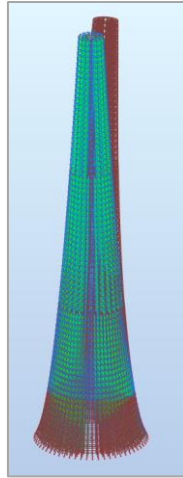
$$R = \pm R_z \pm 0.4 R_x \pm 0.4 R_y$$



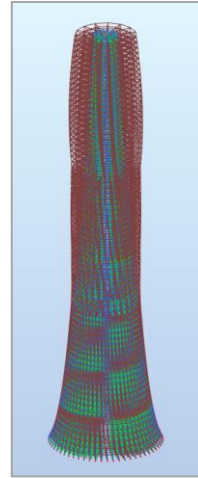
Modal analysis : preliminary results



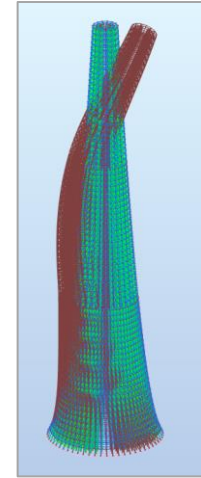
N°1 : 0.05 Hz



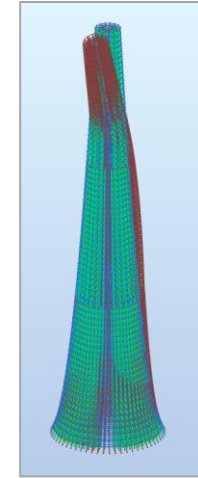
N°2 : 0.05 Hz



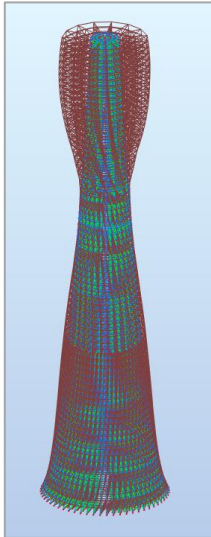
N°3 : 0.11 Hz



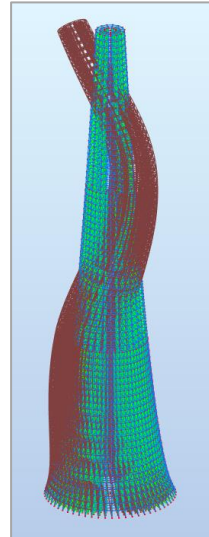
N°4 : 0.11 Hz



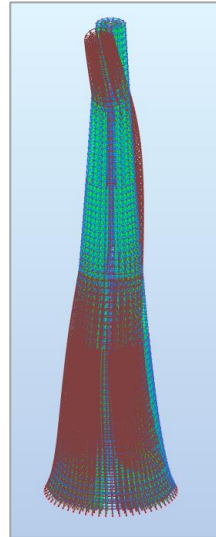
N°5 : 0.11 Hz



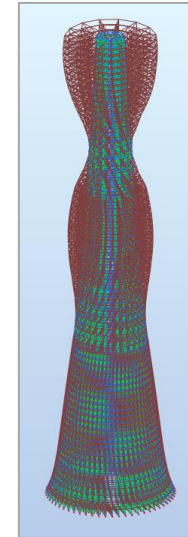
N°6 : 0.17 Hz



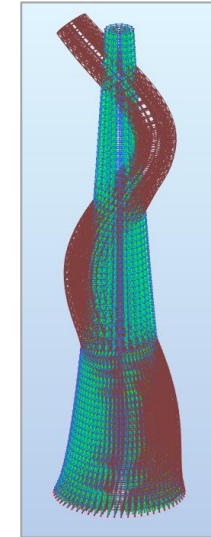
N°7 : 0.18 Hz



N°8 : 0.18 Hz



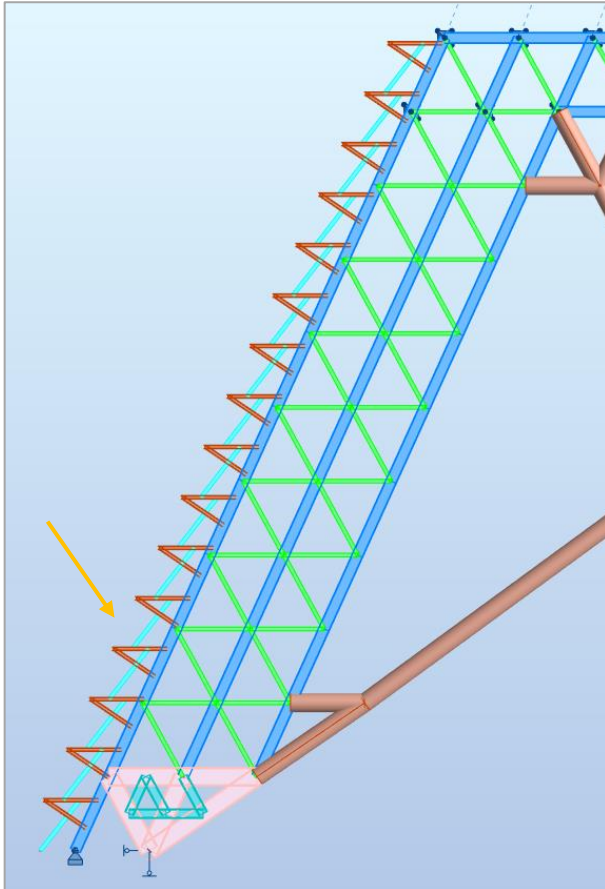
N°9 : 0.24 Hz



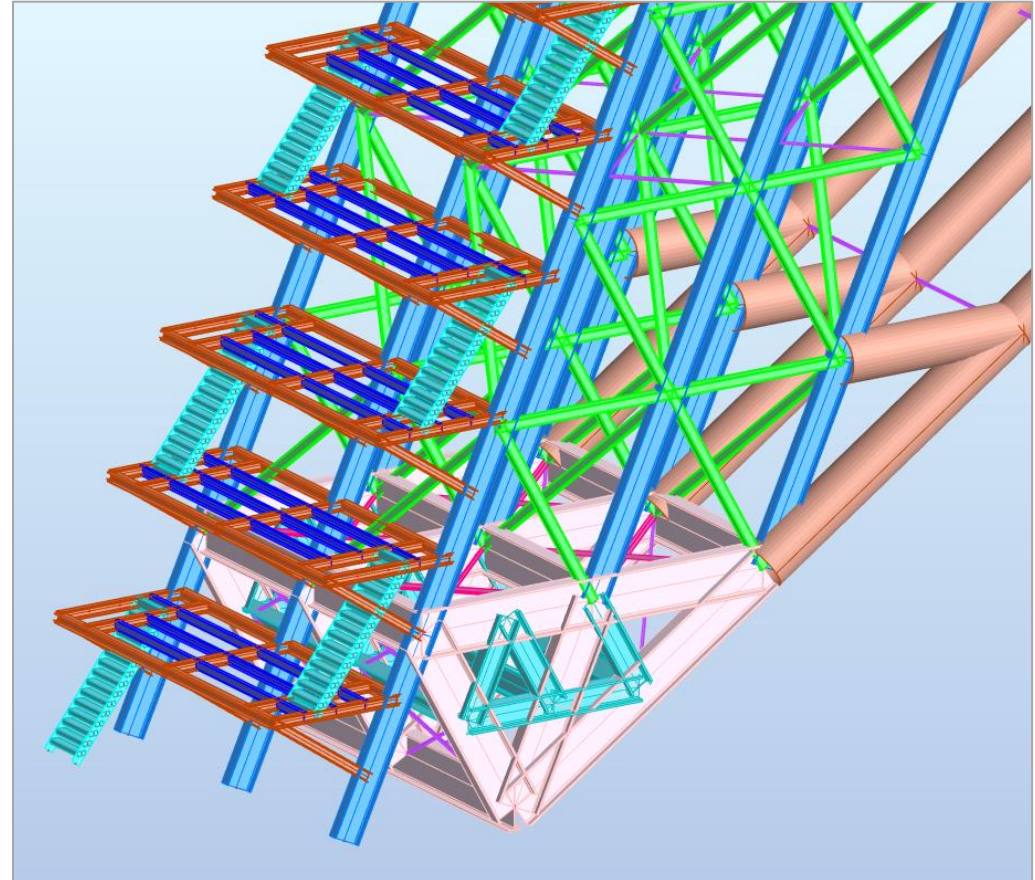
N°10 : 0.28 Hz

Stairs and walkways

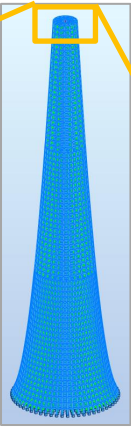
Side view



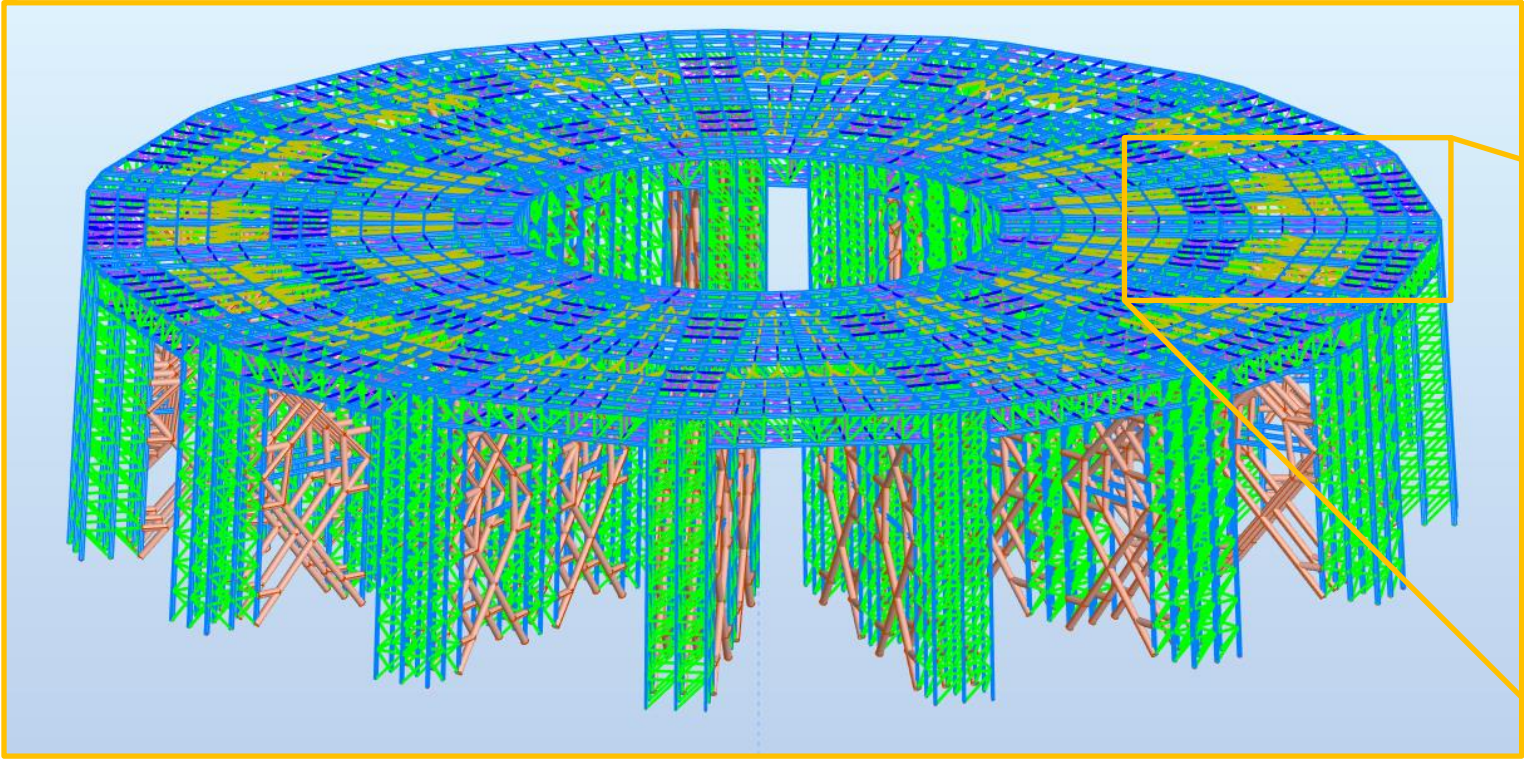
Perspective view



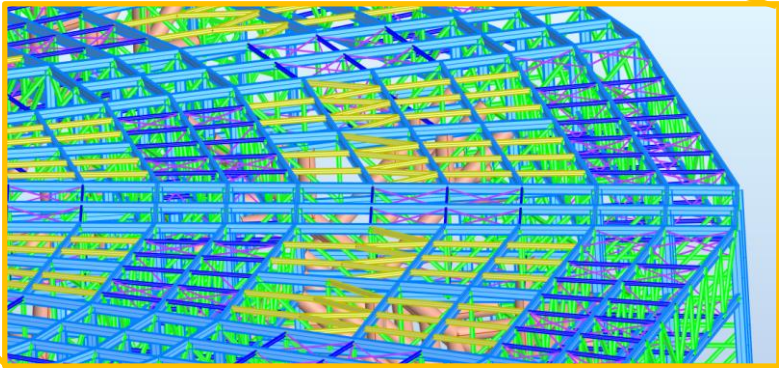
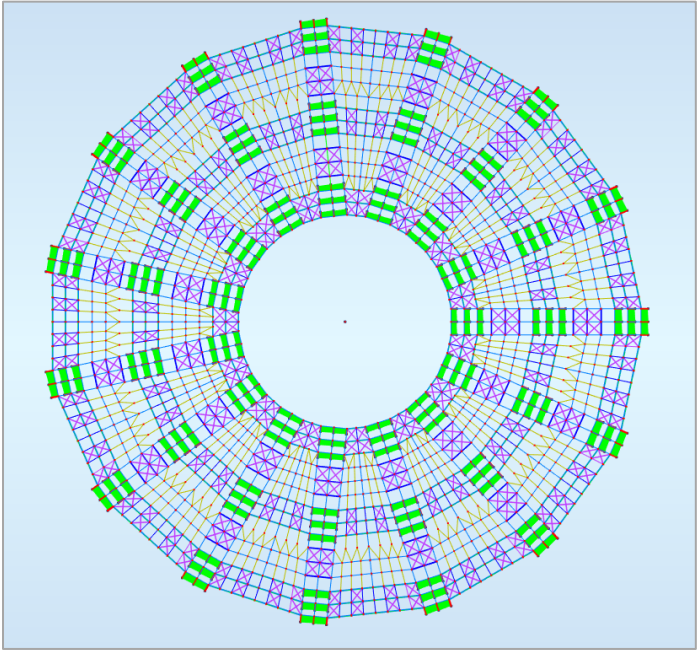
Floor z = +3000 m
(10 300 tons)



Perspective view (23 000 beam elements, 8 000 nodes)

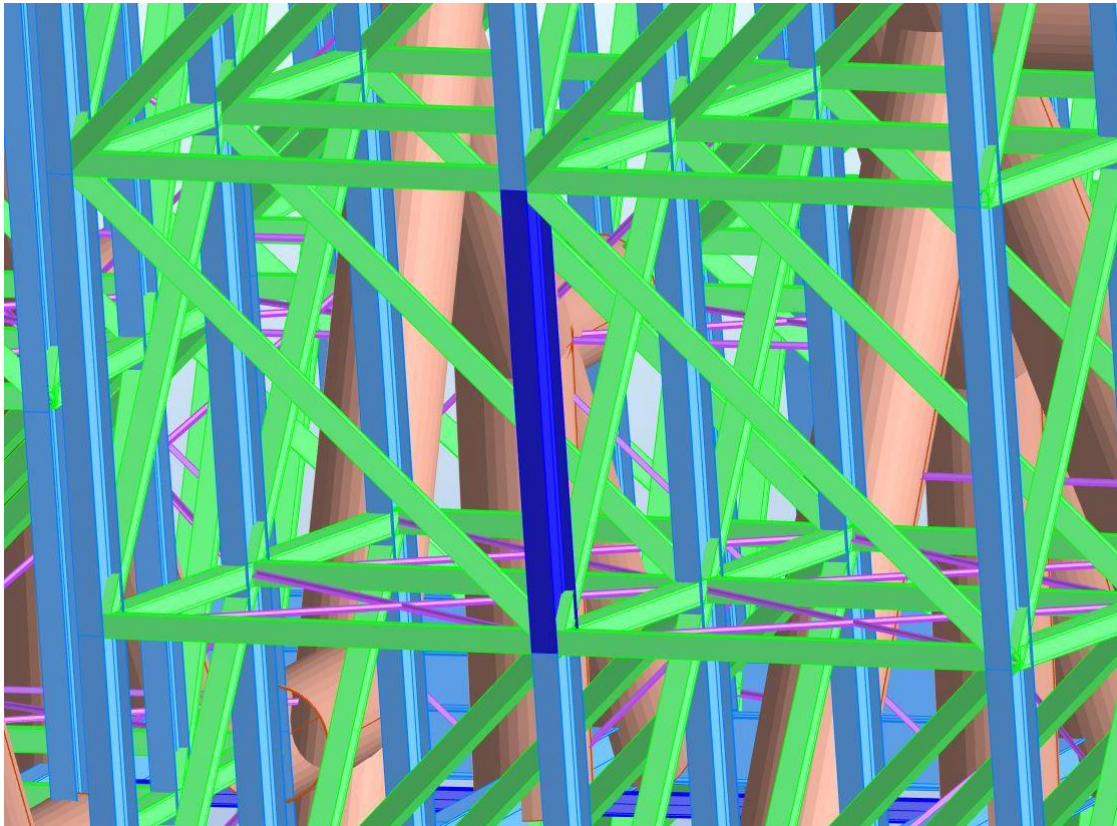


Aerial view

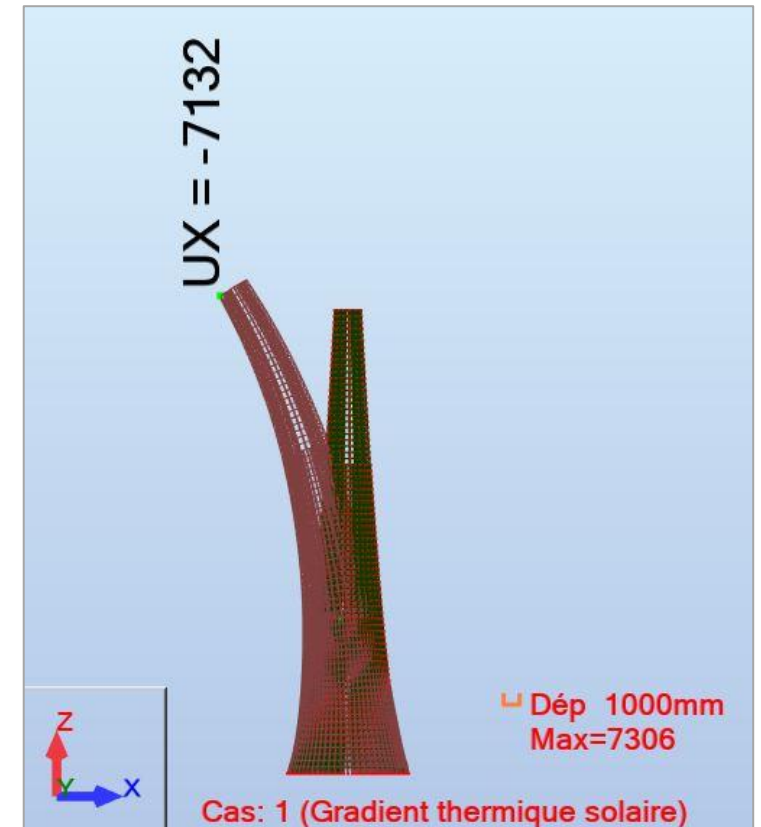


Thermal gradient from the sun

- Shadows from the beams significantly limit the thermal gradient caused by the sun

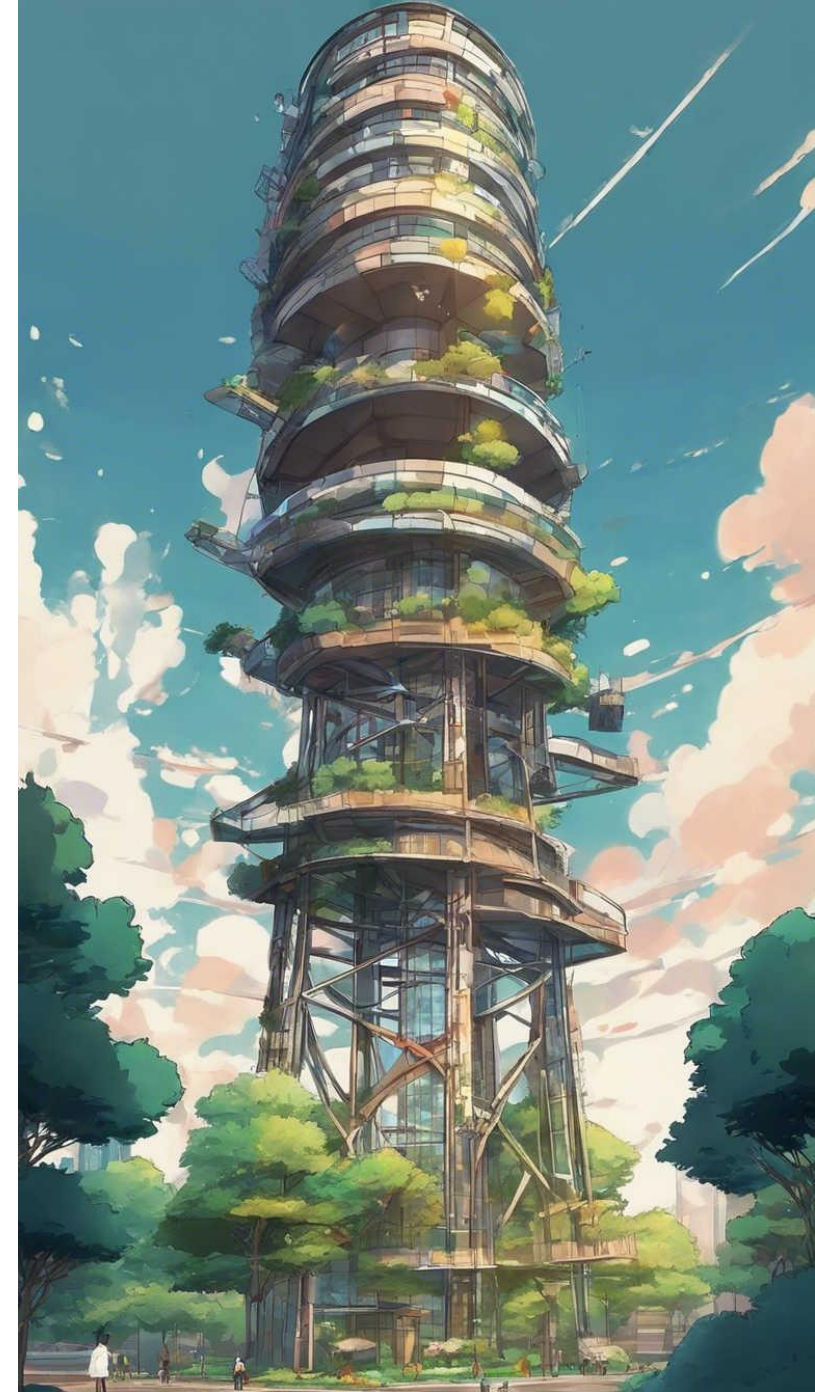


25°C/60°C thermal gradient
(never happens)



I will leave you with this question

- ▶ How can this structure be integrated into socio-ecological needs and sustainability of the future ?





Thank You!

sebastien.besse@cgindustrie.com

+33 (0)6 73 52 02 82

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